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# A PRELTMINARY SKEtch of formula algol 

## by

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## INTRODUCTION

In the information processing sciences a central role is played by programming languages and by the complex information processing programs that we can write from them. The power of programming languages available to the programer often determines whether or not a given programming task can be accomplished without prohibitive expense. As the power of available programming languages increases both the variety of information processing tasks that can be programmed and the ease with which they can be programmed increase correspondingly.

In earlier years algebraic languages, list processing languages and string manipulating languages have existed separately from one another. Recently, formula manipulating languages have evolved; and, In addition, there have been efforts to combine various different kinds of processing in one language.* The design of Formula Algol represents an effort in this direction. Specifically, Formula Algol is an extension to Algol providing formula manipulating, list processing, and limited string processing capabilities. Thus, Formula Algol is a language in which the advantages of these various different kinds of processing are combined, but we anticipate that Formula Algol will be particularly well adapted to algebraic symbol manipulating processes.

[^0]$\Gamma$
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## I. EXPRESSIONS

There are seven different kinds of expressions in Formula Algol. The first three kinds of expressions, namely designational expressions, arithmetic expressions, and Boolean expressions are those of Algol.

In addition, there are four other kinds of expressions in Formula Algol which are not in Algol. These are:
(1) Formula Expressions,
(2) Pattern Expressions,
(3) Symbolic Expressions, and
(4) Tree Expressions.

Every expression has a value. These values have associated types. Types INTEGER, REAL, and BOOLEAN, are already defined in Algol. In addition to these Formula Algol has two new types, FORM and SYMBOL. A. variable declared of type FORM will take on two properties. First, formulas and patterns may be stored into it. Second, it may be used within formula and pattern expressions. Likewise, a variable declared of type SYMBOL may contain lists and may occur in symbolic expressions and tree expressions.

Whereas arithmetic and Boolean expressions have values whose types are always arithmetic and Boolean respectively, such is not the case for formula expressions, pattern
2.
expressions, symbolic expressions, and tree expressions.
By contrast, formula expressions and pattern expressions may take on not only values of type FORM but also any one of the others. Likewise, symbolic expressions and tree expressfons may take on not only values of type SYMBOL but also any one of the others. [Note: This means that formula expressions and pattern expressions may take on values of type SYMBOL, and that symbolic expressions and tree expressions may take on values of type FORM.]

## II. FORMULA MANIPULATION IN FORMULA ALGOL

A. Data Structures for Formulas

In addition to the data structures already in Algoi, Formula Algol introduces some new data structures. Formulas are one of these additional new data structures.

A formula is represented as a list structure composed as follows: The representation is either
(1) an atomic formula variable, or
(2) an atomic constant, or else it is
(3) a combination, consisting of a binary operator, a left half, which is a formula, and a right half, which is a formula (or which is empty in the case of a unary operator which is a binary operator with an empty right half)

For example:
If $X$ and $Y$ have been declared of type FORM, then the expression $3 \times \operatorname{SIN}(X)+(X+Y) \uparrow 2$ is represented by the following list structure:


Formulas need not be only arithmetic and Boolean. In addition, there are four other types of formulas:
(1) conditional formulas (2) assignment formulas (3) procedure formulas, and (4) array formulas. The internal computer representation of all of these formulas is the same. In analogy to the internal representation of arithmetic and Boolean formulas, additional types of binary operators are introduced allowing us to represent conditionals, assignment statements, procedures, and array elements. This is done as follows:
(1) Conditional Formulas

Suppose we have the statement P $\leftarrow$. If $\operatorname{B}$ THEN G ELSE H ;
4.
where $F$ is of type FORM and where the type of $B, G$ and $H$ is immaterial. This creates a formula which we may represent by

in which $\rightarrow$ and EITHER are internal binary operators (meaning that these operators are not part of the alphabet of the source language). The formula is stored into $F$, causing the value of $F$ to become a conditional formula. Later, when we discuss the evaluation of formulas, we will see that the conditional action represented by this formula can be executed when the EVAL operator is applied to F. Here $G$ will become the value of $F$ if $B$ is found to be true and $H$ will be the value of F otherwise.

## (2) Assignment Formulas

Suppose we have the statement $F \leftarrow G . \leftarrow A+B$; where $F$ is of type FORM and the types of G, A and B are any type other than symbol. This creates a formula, which
we may represent by


In which.$\leftarrow$ is a binary operator, and this formula is stored into $F$. Hence, the value of $F$ is an assignment formula. If, at a later time, we apply the EVAL operator to $F$, the assignment of $A+B$ to be the contents of $G$ takes place. Thus, at one point in a program, we may describe the skeleton of an assignment, and at a later time, as a result of some unpredictable running experience, the program may fill in the details and carry out the assignment. The essential theme of this is that we may specify at any point to any desired degree of detail a partial schema for a computation, postponing until later the specification of details dependent on the outcome of further computation which details we cannot predict.

```
(3) Procedure Formulas
    Suppose we have the statement F}\leftarrow TAYLOR.(G,X,N )
where F,G,X, and N are of type FORM. Executing this
```

6. 

statement creates a formula which we may represent by

in which . PROCEDURE is a binary operator, and this formula is stored in $F$. As in the previous case, applying the EVAL operator to $F$ causes the actual execution of the procedure TAYLOR.
(4) Array Formulas

Executing the statement $F \leftarrow B .[I, J, K]$; causes the formula

to be stored in $F$, where .ARRAY is a binary operator. F must be of type FORM, B can be of any type, but it must be the identifier of a previously declared array. Applying the EVAL operator to $F$ with values for $I, J$, and $K$

```
causes the execution of the array access. For example, executing the statements
\[
\begin{aligned}
& \mathrm{A} \leftarrow \mathrm{~L} \cdot[3,4] ; \\
& \mathrm{P} \leftarrow \text { TAYLOR. }(\mathrm{F}, \mathrm{X}, \mathrm{~N}) ; \\
& \mathrm{G} \leftarrow . \mathrm{IF} \text { B THEN A ELSE } P ; \\
& \mathrm{F} \leftarrow \mathrm{~L} \cdot \mathrm{G} ;
\end{aligned}
\]
causes the following formula to be assigned the value of \(F\)
```



```
The value of \(F\) thus represents a postponed assignment to \(L\) of a postponed conditional which if \(B\) is true represents the postponed array access \(L[3,4]\), and if \(B\) is false the postponed procedure execution TAYLOR ( \(\mathrm{F}, \mathrm{X}, \mathrm{N}\) ).
```

8. 

B. Operators for Formulas

Having added formulas as a new type of data structure certain classes of operators are immediately suggested.
(1) Constructors

A formula is always created by writing directly the linearized algebraic expression which represents it. For example, if the formula, $3 \sin x+(x+y)^{2}$, is going to be stored in the formula variable $Z$, we shall write:

$$
z \leftarrow 3 * \operatorname{SIN}(x)+(X+Y) \uparrow 2 ;
$$

After the execution of this statement, $Z$ is a formula variable having a formula value represented by the list structure described on Page 3.

As we will see later the EVAL operator is also capable of being used as a constructor.
(2) Predicates and Selectors

If as a result of some computation a formula has been built up whose structure cannot be predicted in advance, we may precisely determine its structure by the use of predicates. These predicates are sufficient in the sense that, whatever constructions are used to create a formula, the process may be reversed by the choice of a sequence of predicates. In the

```
case of formulas, we call these predicates "patterns".
Patterns are defined by the following BNF syntax equations:
    <pattern>::= <formula expression> == <pattern structure>1
        <formula expression> >> <pattern structure>|
        <identifier>: <formula expression>>>
            <identifier>: <pattern structure>
```

In this definition, a formula expression is compared with a
"pattern structure" to determine whether the expression is an
exact instance of the pattern structure or whether the
expression contains an instance of the pattern structure.
Thus, we write <formula expression> $==$ <pattern structure> to
mean "Is the formula expression an instance of the pattern
structure?", and we write <formula expression>>>
<pattern structure> to mean "Does the formula expression
contain an instance of the pattern structure?" The use of the
<identifier>'s in the definition of a pattern will be explained
later. Pattern structures are defined as follows:
<pattern structure>: :=
<a formula in which some of the primaries may have
been replaced by pattern primaries and some of the
operators may have been replaced by |<variable>|>
10.

> <pattern primary>: $:=$ <unlabelled pattern primary>|
> <variable> : <unlabelled pattern primary>
> <unlabelled pattern primary> $::=$ <type> $\mid$ of (<variable>)|ATOM
> The colon used in the definition of pattern primaries is an extraction operator. It extracts the part of the formula matching the corresponding unlabelled pattern primary. A copy of the extracted part of the formula is assigned as the value of the identifier found to the left of the colon.

Suppose $R$ is a variable declared of type SYMBOL for which the following assignment statement has been executed:
$R \leftarrow /[$ index: J] [operator:,,$+- /]$ [comm:true,false,false];

The effect of executing this statement (as will be explained later when we introduce the list processing features of Formula Algol) is to assign $R$ a description list whose attribute value List follows the first occurrence of the mark / in the above assignment statement. Here, each attribute precedes the colon inside each pair of square brackets and the value list associated with that attribute follows the colon.

Consider now the pattern $F==A:$ INTEGER $|R| B: F O R M$. This pattern will be true in any of the two following cases:


#### Abstract

(1) The first operand of $F$ is an integer and the second is a formula and the main operator is either,+- , or $/$. (2) The first operand of $F$ is a formula and the second operand of $F$ is an integer and the operator is +

In case 1, assuming there was a match, A is assigned the value of the integer, $B$ is assigned the value of the formula, the index $J$ is set to 1,2 , or 3 according to whether the main operator was $t$, -, or / respectively, and this main operator is stored as a data term in the contents of $R$. In case 2 , since the value of the attribute "comm" on the description 1ist of $R$ is the 1ist [true, false, false], the pattern also stands for comatative instances of the right and left operands about any of the operators ,+- , or / whose corresponding Boolean values following the attribute "comn" are set to true. Thus, in this case, + is a commutative operator and - and / are not. Therefore, only commutative instances about the operator + are considered. We note that [comis true, false, false] need not appear on the description list of R at all, in which case no commutative instances of any operator will be considered. Later we can use the construction $|<R|$ in an expres. sion in place of an operator. The operator that $|\langle R\rangle|$ stands for is exactly the one which was extracted during previous pattern matching. Alternatively, $R$ may be assigned any operator by the assignment statement $R \leftarrow+$; and $|<R>|$ may be used in the same fashion.


12. 

The following are examples of patterns:

Example 1. Let $A, B, X, Y$, and $Z$ be declared of type FORM, and let $R$ be declared of type REAL. Suppose the statement

$$
X \leftarrow 3 * \operatorname{SIN}(Y)+(Y-Z) / R+2 * R
$$

has been executed.
Consider now the statement:

IF $X \gg A:$ INTEGER * B: SIN(FORM)
THEN $Z \leftarrow 2 * B+A ;$

Since the pattern $\gg A: I N T E G E R * B: S I N(F O R M)$ is true, the assignment $Z \leftarrow 2 * B+A$ will be executed, assigning as the value of $Z$ the formula $2 *$ SIN (Y) +3 because $A$ has the value 3 and $B$ the value $\operatorname{SIN}(Y)$.

Example 2. Let $X$ be of type SYMBOL, $A, B, Y, M, T, G$, and $P$ be of type FORM, and let $D$ be of type BOOLEAN. Then executing the statements:

$$
\begin{aligned}
& \mathrm{X} \leftarrow[\text { REAL, INTEGER, BOOLEAN }] ; \\
& \mathrm{G} \leftarrow \mathrm{Y}+8 *(\mathrm{M}-\mathrm{T}) ; \\
& \mathrm{P} \leftarrow \mathrm{FORM}+\mathrm{A}: \mathrm{OF}(\mathrm{X}) * \mathrm{~B}: \text { FORM } ; \\
& \mathrm{D} \leftarrow \mathrm{G}==\mathrm{P} ;
\end{aligned}
$$

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| :---: | :---: |
| ; |  |
| $\Gamma$ |  |
| 1 | 13. |
| F | causes $D$ to be set to true because the pattern $G==P$ is |
| 1 | true, and causes $A$ to be set to 8 and $B$ to be set to M - T. |
| 1 | In this example, we observe that in the definition of a |
| $\cdots$ | pattern primary a type may be replaced by a symbol having |
| 1 | a list of types as contents. |
| $\cdots$ | Suppose that we wish to extract either the name or the |
|  | parameters of a procedure formula or that we wish to extract |
| $\cdots$ | either the name or the subscripts of an array formula. To do |
| $\Gamma$ | these, we may write patterns of the form |
| + | $F=X:$ FORM. (P1:FORM, P2 : FORM) |
| $\Gamma$ | $\mathrm{F}==\mathrm{X}:$ FORM. [ $\mathrm{X} 1:$ INTEGER, X $2:$ INTEGER] |
| $r$ | Here X will contain the name of the procedure or array and |
| ! | P1, P2, X1, and X2 w111 contain the parameters or subscripts in |
| $\cdots$ | the event that there is a match. Extraction from conditional |
|  | formulas and assignment formulas is entirely analogous. |
| F | We now explain by means of an example the function of the |
| - | colon in patterns of the form |
|  | <identifier> : <formula expression>>> |
| $\Gamma$ | <identifier> : <pattern structure> |
| $\cdots$ | Suppose we have executed the statements |

14. 

$$
\begin{aligned}
& \mathrm{F} \leftarrow 2^{*}(\operatorname{SIN}(X \uparrow 2+Y \uparrow 2)+\cos (X \uparrow 2-Y \uparrow 2)) / 5 ; \\
& G \leftarrow \operatorname{SIN}(\mathrm{FORM})+\operatorname{COS}(\mathrm{FORM}),
\end{aligned}
$$

where all variables used are of type FORM. Then A: $F \gg T: G$ is a pattern with value true. The value of $T$ will replace the first instance of $G$ in $F$, i.e., the expression $\operatorname{SIN}(X \uparrow 2+Y \uparrow 2)+\operatorname{Cos}(X \uparrow 2-Y \uparrow 2)$ [this being the first sub-expression of $F$ matching the pattern $G$ ] and $A$ is assigned the expression $2 * T / 5$. In this case, the atomic symbol $T$ is contained in the formula


Thus, $A$ is the same as $F$ with the first sub-expression of $F$ matching $G$ replaced by the value of $T$.
3. Evaluation Rules

We may think of formulas as abstractions of computations. By manipulating formulas we alter the computations they represent. At some point in the execution of a program, we may wish to carry out the computation represented by a formula. To do this, we could substitute values for those variables whose values are not assigned, and those values will be combined according to the computation expressed by the formula resulting
in an evaluated formula. In order to accomplish the above we have the EVAL operator.

If we have a formula consisting of formula variables joined by arithmetic operators, then, if we assign each of the formula variables a numerical value, the result of evaluation of the formula will be a number. Hence, the evaluation of an arithmetic formula by complete substitution of numbers for formula variables is a computation carrying the set of numbers substituted into a number. Analagously, substitution of Boolean values for formula variables in a Boolean formula produces a Boolean value.

On the other hand, we need not substitute arithmetic or Boolean values for formula variables, but rather, we can substitute other formulas. Thus, in this case, evaluation of the formula, instead of collapsing it to a single value, expands it to an enlarged formula. Hence, EVAL may be used as a constructor.

A third use of EVAL is that of producing trivial simplifications in a formula without altering its value and without substitution.

A final use of EVAL is to carry out the array access or procedure call indicated by a "dot array formula" or a "dot procedure formula", or to carry out the assignment of a value or the choice of a value indicated by a "dot assignment formula" or a "dot if formula".
16.

For example: If the formula $X$ has the value
$\mathrm{X}=$


Then the expression EVAL $X$ will produce the number 11 as value, as in the example $V \leftarrow 3+$ EVAL $X$, after which $V$ has the value 14. $X$ is not altered by EVAL $X$.

These uses of EVAL represent extreme cases. In a given application they may be combined. Thus evaluation of a formula may produce partial collapsing, partial expansion, and some trivial algebraic simplification simultaneously. [Note: substitution is always simultaneous.]

The syntax and interpretation of evaluation formulas is as follows:

```
<EVAL formula> ::= EVAL <variable> |
            EVAL <bound variables> <expression> <list of values>
<list of values> ::= (<actual parameter list>) | ([<variable>])
<bound variables> ::= (<variable list>) | ([<variable>])
<variable list> ::= <variable> | <variable list> ,<variable>
```

Consider a statement of the form:

$$
\begin{equation*}
D \leftarrow \operatorname{EVAL}\left(X_{1}, X_{2}, \ldots, X_{m}\right) F\left(Y_{1}, Y_{2}, \ldots, Y_{n}\right) \tag{1}
\end{equation*}
$$

where $n \geq 1$, and $m \geq 1$.
Then it is the case that:
(a) $F$ must be a variable declared of type FORM; nevertheless at execution time it may become any type.
(b) If the current value of $F$ is not an expression, then the effect of [1] is precisely that of $D \leftarrow F$.
(c) If the current value of $F$ is an expression, then $D$ will have the value obtained by the execution of the piece of code produced by the interpretation of $F$ as an arithmetic or Boolean expression, in which were substituted $Y_{i}$ for all of the corresponding occurrences of $X_{i}$ in $F$, for all $i \leq m$. The substitution is made in accordance with the following rules. If
$X_{i}$ is not of type FORM, $X_{i}$ is ignored; or if
$X_{i}$ is of type FORM, but does not occur in $F, X_{i}$ is
is ignored, or if
$X_{i}$ is of type FORM, and it occurs in $F$, but $i>n$,
$X_{i}$ is ignored, or if
$X_{i}$ is of type FORM, and it occurs in $F$, with $i \leq n$, then $X_{i}$ is replaced by $Y_{i}$.
18.
(d) $X_{i}$ may be an expression of any type.
(e) The expression $F$ is not changed as a consequence of the execution of EVAL.
(f) D must be of type FORM, unless the evaluation of $F$ produces a numerical or logical value.

The evaluation process creates a new expression which may be ultimately of any type, depending on current values.

Executing EVAL $F$ where $F$ is an assignment formula, a procedure formula or an array formula, respectively, causes the assignment to be executed, the procedure to be evaluated, and the array element to be accessed respectively.

When evaluating a conditional formula, only if the Boolean formula in the if clause collapses to a Boolean value will the conditional formula be executed. This process requires substitutions. If, on the other hand, the Boolean formula does not collapse to a single value, then another conditional formula is constructed with the corresponding substitutions.
C. Remarks

When the value of a formula is given by an assigment statement later assignment statements do not alter the originally assigned formula. Assignments are not retroactive. For example,

$$
\begin{aligned}
& \mathbf{Y} \leftarrow \mathbf{A}+\mathbf{B} ; \\
& \mathrm{X} \leftarrow \mathrm{Y}+3 ; \\
& \mathrm{Y} \leftarrow \mathrm{~F}+\mathrm{G} ;
\end{aligned}
$$

# After the execution of these statements $X$ has as its value the formula and not 



In symbol manipulation the reverse is true. As we will see later, during the discussion of the list processing features of the language, after the execution of the following three statements:

$$
\begin{aligned}
& Y \leftarrow[A, B] ; \\
& X \leftarrow[Y, 3] ; \\
& Y \leftarrow[F, G] ;
\end{aligned}
$$

the value of the expression $\langle$ IRST of $\langle\varnothing\rangle$, which means "the contents of the first element of the list stored as the contents of $X^{\prime \prime}$, will be the list $[F, G]$ and not the list $[A, B]$.

Experience indicates that those with a background in list processing languages confuse the above mentioned point when dealing with Formula Algol for the first time.
20.
III. LIST PROCESSING IN FORMULA ALGOL
A. Symbolic Data Structures

There are three kinds of symbolic data structures: symbols, list structures, and description lists.
(1) Symbols

A variable, S, in Formula Algol, which is declared to be a symbol acquires the following properties:
(a) $S$ names a storage location into which symbolic data structures may be stored.
(b) $S$ may have a description list attached to it into which attributes and values may be entered and retrieved.
(c) $S$ may be used as an atom in constructing symbolic data structures.

Note: Unlike other types of variables in Formula Algol, S does not have a value. The contents of $S$ is not the vaiue of $S$. Instead, the contents must be accessed by applying an operator to $S$, namely, by enclosing $S$ in contents brackets, $\langle S\rangle$. Whereas writing the real variable $R$ in a statement such as $T \leftarrow 2 * R$; causes the value of $R$ to be used, writing the symbol $S$ in the list [ $A, B, C, S]$ causes $S$ itself to be entered into the list, and not some value or structure which $S$ stands for.
(2) List Structures

Symbols may be concatenated into a list by writing them one
after another, and by separating them with commas. This list may be assigned as the contents of another symbol by executing an assigment statement. E.g. VOWEL $\leftarrow[A, E, I, O, U]$;

An item concatenated into a list need not be a symbol. It may be any expression legal in Formula Algol. For example: let $X, Y$, and $Z$ be formulas, let A, B, and C be Boolean, let U, V, and $W$ be real, and let $R, S$, and $T$ be symbols. Then the following assigment statement is legal.
$S \leftarrow[X+S I N(Y), 3+2 * U$, IF B THEN R ELSE $T,[R, T, R],-36]$; At the time this statement is executed, each expression on the right is evaluated, and the 1ist of values is stored into the contents of $S$. In effect, automatic data term declaration results from storing non-symbolic values into list structures. Note that the second from the last item in the above expression is the quantity $[R, T, R]$. This becomes a sublist of the list stored into S. Hence, the expression stored into $S$ is, in reality, a list structure. For this reason, the expression on the right hand side of the above statement is called a tree expression. Tree expressions represent 1ist structures into which values of any type may be entered and retrieved. The operators for manipulating tree expressions will be introduced subsequently.
(3) Description Lists

A description list is a sequence of attributes and values.
22.

Each attribute is followed by a list of values associated with it. This value list may contain more than one member, it may contain only one member, or it may be empty. A description list is always attached to a symbol and becomes permanently bound to it. Any symbol may become an attribute, and, in addition to symbols, the value of any expression legal in Formula Algol may become a value. Let $A_{1}, A_{2}$, and $A_{3}$ be symbols used as attributes, and let $V_{m n}$, for $m$ and $n$ integers, stand for values. Then an example of a description list is

$$
/\left[A_{1}: V_{11}, V_{12}, V_{13}\right]\left[A_{2}: V_{21}\right]\left[A_{3}: V_{31}, V_{32}, V_{33}, V_{34}\right]
$$ The operators for entering and retrieving attributes and values in description lists will be introduced subsequently.

B. Operators for Accomplishing List Processing

The introduction of symbolic data structures into Formula Algol makes mandatory the existence of certain classes of operators among which are first, constructors, to create them; second, selectors, to gain access to various parts of them; and third, predicates; to determine the structure of those whose structure is unknown.

1. Constructors

The most elementary and direct method of creating both tree expressions and description lists is to write them out linearly and to store them into the contents of some symbol. E.g. Assume that

| $\Gamma$ |  |
| :---: | :---: |
|  |  |
|  |  |
| $\Gamma$ |  |
|  | 23. |
| $\Gamma$ | all identifiers in the following statement are symbols: |
| $[S \leftarrow[A, B, C, D]$; |  |
| $S \leftarrow /$ [types: mu, pi, rho] [ancestors: orthol, para5] [color: |  |
| green]; |  |
| The first statement creates the list [ $A, B, C, D]$ and stores it as |  |
| the contents of $S$. The second creates the description list |  |
| / [types: mu, pi, rho] [ancestors: orthol, para5] [color: green] |  |
| and attaches it to the symbol $S$. |  |
| Methods of creating and altering both tree expressions and |  |
| description 1ists by means of editing statements and value entry |  |
| $\Gamma$ | statements will be introduced after the introduction of selectors. |
| 2. Selectors |  |
| Symbolic expressions may, upon evaluation, yield both symbols |  |
| $\Gamma$ | and lists of symbols as values. They may also, upon evaluation, |
|  | yield arithmetic, Boolean, and formula values. Anywhere a symbol |
| - | appears it may be replaced by a symbolic expression, which, upon |
| - | evaluation, yields a symbol as a result. Likewise, anywhere a list |
| 1 | of symbols appears it may be replaced by a symbolic expression, |
| T | which, upon evaluation, yields a list of symbols as a result. |
|  | Selectors are operators which are applied to a symbolic data struc- |
| 1 | ture to gain access to a part of that data structure. The following classes of selectors are available: |

24. 

(a) Retrieval of the contents of a symbol.

Suppose $S \leftarrow[A, B, C]$; has been executed. Then $S$ contains the list [ $A, B, C$ ]. To access the contents of $S$ we form the expression $\langle S\rangle$. This is read "the contents of $S^{\prime \prime}$. It is a symbolic expression whose value is, In this case, the list $[A, B, C]$. If we execute the statements: $T \leftarrow S$; and $S \leftarrow[A, B, C]$; then $\langle T\rangle$ is a single valued symbolic expression with value $S$, and $\langle\langle T\rangle\rangle$ is a list valued symbolic expression with value $[A, B, C]$. The angular brackets, $\rangle$, may be nested arbitrarily many times to give arbitrarily many levels of indirection.
(b) Retrieval of values from a description list.

Suppose the statement
$S \leftarrow /$ [types: mu, pi, rho] [ancestors: orthol, para5] [color: green] ;
has been executed causing a description list to have been created and to have been attached to $S$. Suppose we wish to determine the values of the attribute "ancestors" on the description list of $S$. To do this we write "THE ancestors 0 F $\mathrm{S}^{\prime \prime}$. This is a list valued symbolic expressfon having the list [ orthol, para5] as value. The expression "THE color OF S " is a single valued symbolic

| $\Gamma$ |  |
| :---: | :---: |
|  | 25. |
| [ expression having the symbol "green" as value. |  |
| $\Gamma$ | (c) Retrieval of elements and sublists of a list. |
|  | Suppose the statement $S \leftarrow[X, A, X, A, A, X, A, A, A, X] ;$ |
| $\Gamma$ | has been executed causing the list shown to be stored as |
|  | the contents of $S$. We may access the various symbols on |
| $\Gamma$ | this list by means of "selection expressions". Selection |
| $\Gamma$ | expressions consist of selector operators applied to list |
|  | valued symbolic expressions. We know already that < S > |
| $\Gamma$ | Is a list valued symbolic expression having the 1ist |
|  | $[X, A, X, A, A, X, A, A, A, X]$ as a value. Hence, the expression |
|  | 3RD OF < S > is a single valued symbolic expression having |
| $\Gamma$ | the value X . Likewise, LAST $\mathrm{OF}<\mathrm{S}>$ has the value X , |
|  | whereas 2ND BEFORE LAST $\mathrm{OF}\langle\mathrm{S}>$ has the value $A$, and |
| $\Gamma$ | whereas 2ND BEFORE 3RD X OF $\langle\mathrm{S}\rangle$ has the value $A$. |
|  | Selection expressions need not have single values. For |
|  | example: the expression FIRST $4 \mathrm{OF}<\mathrm{S}>$ has the list |
|  | [ $X, A, X, A$ ] as value, and the expression |
|  | between first $X$ and 1st before last $X$ OF $<S>$ has the |
| $\Gamma$ | list $[A, X, A, A, X, A, A]$ as value. Selectors may be compounded to access sublists and their elements. Suppose |
|  |  |
|  | the statement $S \leftarrow[A,[X, X,[A, A], X], A]$ has been |
|  | executed. Then the expression 2 ND OF $\langle\mathrm{S}\rangle$ is a list |

26. 

valued symbolic expression with the list $[X ; X,[A, A], X]$ as value, whereas the expression 3RD OF 2ND OF < S > has the list $[A, A]$ as value, and whereas the expression LAST OF 3RD OF 2ND OF $<S>$ is a single valued symbolic expression with the value $A$.
3. Predicates

Predicates for determining the structure of 1 ists and 1ist structures are of two kinds: "1ist patterns" and "relations". List patterns use the mechanisms found in COMIT to test whether a innear list is an instance of a certain linesr pattern. The constituent selector list describes the pattern being tested for, and is composed of a sequence of constituent selectors separated by commas. The symbols $\$$, and $\$ \mathrm{n}$ may be used as constituent selectors with the same significance as in COMIT [viz. \$ stands for any arbitrary number of successive constitutents, and $\$ \mathrm{n}$ stands for n consecutive arbitrary constituents]. If a symbolic expression is used as a constituent selector, its value is first computed, and if that value is a list, each element of the list becomes one of the consecutive constituent selectors in the constituent selector list. Other kinds of elements, to be introduced later, may also become constituent selectors.

A list pattern compares the list determined by a list valued symbolic expression to a linear pattern described by a constituent
28.
a constituent selector list is preceded by a variable declared of type SYMBOL followed by a colon, then the corresponding constituent in the list being tested, in the event that there is a match, is inserted into the contents of that symbol variable. The contents may be accessed at any later point in the program.

Example 2. As in the previous example, suppose the statement $S \leftarrow[A, B, C, D]$ has been executed where all variables are symbols. Then executing the statement

TF < S $\rangle$ HAS $T: \$ 2, V: \$ 2$ THEN $\mathrm{S} \leftarrow[\langle\mathrm{V}\rangle,\langle\mathrm{T}\rangle]$;
changes the contents of $S$ to be the list $[C, D, A, B]$. Furthermore, $\langle T\rangle$ is the list $[A, B]$, and $\langle V\rangle$ is the list $[C, D]$.

Relations constitute a second class of predicates. The following kinds of tests are available:
(a) Equality Relations

If we have two symbolic expressions we may test whether their values are equal by means of the relation <symbolic expression> $=$ <symbolic expression>. The values of the symbolic expressions may be single symbols, lists of symbols, formulas, or values of any other type. Naturally if the values of the two symbolic expressions are non-conformable data structures the result of the predicate will be false.
(b) Testing for types

A single valued symbolic expression having a value whose type is unknown may be used in the relation <symbolic expression> IS <restricted type> in order to determine the type. A restricted type is either REAL, INTEGER, BOOLEAN, HALF, LOGIC, FORMULA, SYMBOL, or SUBLIST.

For example: Suppose R is REAL, $B$ is BOOLEAN, $F$ is FORM, and $A, B, S$, and $T$ are SYMBOL. Suppose further that the statement $S \leftarrow[R, B, F,[A, B], T]$; has been executed. Then

> the relation $1 S T O F<S>$ IS REAL $\quad$ is true
> the relation $2 \mathrm{ND} O F<S>$ IS REAL $\quad$ is false
> the relation $3 \mathrm{RD} O F<S>$ IS FORM is true
> the relation $4 \mathrm{TH} O F<S>$ IS SUBLIST is true, and
> the relation LAST OF $<S>$ IS SYNBOL is true.
(c) Testing for membership in a class

Formula Algol permits sets to be defined by means of class definitions. For example, suppose the statement $V \leftarrow[A, E, I, O, U]$ has been executed. Then the statement $\operatorname{LET}(\mid$ VONEL $\mid)=[\mathbf{X} \mid \operatorname{AMONG}(X, V)] ;$
defines the set of all vowels, (|VOWEL|), where AMONG ( $P, Q$ ) is a Boolean Procedure which is true if $P$
is an element of the list contained in $Q$, and false otherwise. Let us now suppose that, having sometime previously executed the statement $S \leftarrow[A, B, C]$, we execute the statement

IF 1 ST OF < S > IN ( $\mid$ VOWEL $\|$ ) THEN GO TO exit; The relation 1 ST OF $\langle S\rangle$ IN ( $\mid$ VOWEL $\mid$ ) will be evaluated by first computing the value of the expression 1 ST OF $<S\rangle$, which is the symbol $A$, and second by substituting $A$ for the formal parameter $X$ in the class definition of ( | VOWEL \|) . This results in the Boolean procedure AMONG ( A,V ) being executed, the value of which is true. Thus $A$ is in the class ( $\mid$ VOWEL $\mid$ ), and the relation 1 ST OF < S > IN ( $\mid$ VOWEL $\|$ ) is true. This causes us to GO TO exit in the above statement.

Class definitions may consist of Boolean combinations of other defined classes. E.g. LET $(|A|)=(|B|) \wedge(|C|)$; is legal provided ( $|B|$ ) and ( $|C|$ ) are elsewhere defined. Another example of a class definition would be LET $(\mid$ EMPTY $\mid)=[\mathbf{X} \mid \underline{\text { false }}] ;$

This defines the empty set.
Class definitions may be used as constituent selectors in list patterns. When this is done, the constituent
31. matching the class definition is tested for membership in the class. If the result is true the list pattern continues to be matched against the list being tested. If the result is false, the list pattern fails to match the list being tested. E.g. $<S>\operatorname{HAS} D,(|\operatorname{VOWEL}|)$, $\$$ is a legal list pattern which tests the list contained in $S$ to see if it is of the form $D$, followed by a vowel, followed by any arbitrary number of arbitrary constituents.
4. Other Operators and Statements

There are four species of statements which remain to be introduced. These are "value entry statements", "editing statements", "push down and pop up statements", and some additional new types of "for statements". We will discuss them in the order given.
(a) Value entry statements

Value entry statements enter values on description lists. They supplement the role performed by assignment statements in this regard. Suppose that $S \leftarrow /$ [types: mu, pi, rho] [ color: red] has been executed. Then if we execute the statement: THE color OF S IS green; we replace the value of the attribute "color" on the description list of $S$ with the new value "green". This
32.
yields the altered description list /[types: mu, pi, rho] [color: green] as a resuit. On the other hand, we could have executed the statement: THE color OF S IS ALSO green. Instead of replacing the color "red" with the value "green" the latter statement appends the value "green" to the value list following the attribute "color". This yields /[types: mu, pi, rho] [color: red, green] as a result. Finally, we may use value entry statements to delete values from value lists of specific attributes. Executing the statement: THE types OF S IS NOT pi; alters the above description list to be of the form /[types: mu, rho] [color: green].
(b) Editing statements

Editing statements are used to transform, permute, alter, and delete elements in lists. Suppose $S \leftarrow[X, A, A, X]$ has been executed. Then the statement INSERT Y BEFORE LAST $O F<S>$ changes $<S>$ to look like $[X, A, A, Y, X]$. Similar1y, the statement INSERT [ Y, Z ] (AFTER 1ST OF, BEFORE LAST $O F\rangle<S>$ changes $<S>$ to look like $[X,[Y, Z], A, A,[Y, Z]$, $X$ ]. The statement DELETE 3RD BEFORE LAST OF $<S>$ alters $<\mathrm{S}\rangle$ to look like $[\mathrm{A}, \mathrm{A}, \mathrm{X}]$, and DELETE ALL $\mathrm{A} O \mathrm{O}\langle\mathrm{S}\rangle$ causes $\langle S\rangle$ to be changed to $[X, X]$. In a similar vein,
the statement ALTER ALL $A O F<s>$ TO [ $C, C$ ] changes $\langle\mathrm{S}\rangle$ to look like [ $\mathrm{X},[\mathrm{C}, \mathrm{C}],[\mathrm{C}, \mathrm{C}], \mathrm{X}]$. Finally, the statement COPY FIRST 3 OF $<\mathrm{S}>$ AFTER LAST OF $<T>$ would have the effect of appending [ $X, A, A$ ] to the tail of the list given by $\langle T\rangle$. These examples do not exhaust all possible syntactic combinations permissible in editing statements, rather, they exemplify some of the editing operations that are possible.
(c) Push down and Pop up Statements

The contents of any symbol may be regarded as a push down stack. If $S \leftarrow[A, B, C]$ has been executed. Then $\downarrow S$ is a statement, which when executed, pushes the entire contents of $S$ down one level. Picturing the contents of $S$ as a description list / [ CONT: A, B,C ], we may also picture the effect of $\downarrow \mathrm{S}$, which is to insert a stack marker on top of the contents, transforming the above picture to $/[\operatorname{CONT}: \mid A, B, C]$. If we now execute $S \leftarrow[C, D]$, the latter picture transforms to / [CONT: C,D|A,B,C]. Here, the value of $\langle S\rangle$ is the list [ $C, D$ ]. The lower levels of the push down stack are inaccessible to the operation of extracting contents until a pop up statement has been performed. Executing the statement is then transforms
34.
/ [ CONT: C,D | A, B,C] into / [ CONT: A, B,C], and now the value of $\langle S\rangle$ is $[A, B, C]$. Whenever the contents of $S$ is empty, the expression $<S>$ has the value NIL. Thus, should $S$ be popped too many times, nothing will remain in the push down stack and the contents of $S$ will be NIL. The push down operator, $\downarrow$, and the pop up operator, $\uparrow$, may be applied any number of times in succession, as in the examples $\uparrow \uparrow \uparrow S$, and $\downarrow \downarrow$. There is no limit to the number of levels a push down stack may have.
(d) Additional Types of For Statements

We may wish to generate the elements of a list one by one in order to assign them to the controlled variable in a for-statement. For this purpose the for-1ist elements, ATTRIBUTES OF S, and ELEMENTS OF $\langle\mathrm{S}\rangle$ are introduced. Here attributes on the description 1ist of $S$ are generated in the order they occur by ATTRIbUTES OF S , and ELEMENTS OF $<S\rangle$ generates the successive elements of the list $<S\rangle$. In the latter case $<S>$ may be replaced with any list valued symbolic expression.

Parallel generation is also permissible. If $S \leftarrow[A$, $B, C], T \leftarrow[D, E]$, and $U \leftarrow[F, G, H, I]$ have been executed, then executing the statement

36.

In the case of the last two, the procedures have FORM and SYMBOL values respectively.

There will be available to the programmer a number of standard 1ist processing library functions such as COUNT(L), which counts the number of elements on the 1 ist $L$ and gives the result as its value, EMPTY(L) which is true if $\langle\boldsymbol{L}$ is empty and false otherwise, AMONG ( $X, L$ ) which is true if $X$ is an element of the list contained in $L$ and false otherwise, $\operatorname{CREATE}(n, L)$ which inserts a list of $n$ created internal symbols as the contents of $L$, these symbols being taken from the list of available space, ERADL(S) which erases the description list of $S$, and several others.

In addition to having values, formulae may have description 1ists attached. This is done by assignment statements. E.g. $F \leftarrow /$ [ properties: continuous, differentiable].

As in the case of symbols, value retrieval statements and value entry statements may be used to alter and retrieve attributes and values from such description lists.
F FORM PROCEDURE OERV(G,X); FORM G;X;
COMMENT: THIS PROCEDURE COMPUESS THE DERIVATIVE OF G WITH RESPECT
TO X ITERATIVELY. ( IN REFERENCE[4] A RECUSSIVE OIFFERENTIATION
WE HAVE TWO FORMULA ARRAYS,F AND D. F(I) CONTAINS A FORMULA
TO BE DIFFERENTIATED, AND D[I] WILL CONTAIN THE EXPRESSION OF
ITS DERIVATIVE. THIS DERIVATIVE IS CONSTRUCTED, IN GENERAL,
IN TERMS OF THE DERIVATIVES OF THE OPERANDS OF F[I]. THESE
OPERANDS WILL BE STORED IN SOME OTHER F[K] AND F[J] WITH K,J>I.
IN THE EXPRESSION OF D[I] WE DO NOT USE THE VALUES OF O[K]
AND D(J) RATHER WE USE THE ACCESSING FUNCTIONS (FORMULA ARRAY
EXPRESSIONS). ULTIMATELY THE PROCESS OF DIFFERENTIATION REDUCES
TO DIFFERENTIATION OF X AND OF CONSTANTS, THUS CAUSING IT TO TERMINATE.
WHEN THIS HAPPENS WE COLLECT BACKWAROS BY MEANS OF EVAL;
BEGIN SYMBOL T,ANY; INTEGER I,J,K; FORM ARRAY F,D[1:1001;
SWITCH L \leftarrowL1,L2,L3,L4,L5;
T + / [INDEX :K ] [OPERATOR :+,*,*,//,t];
ANY \& [REAL,INTEGER,HALF,FORM];
F[1]-G; J-1;
FOR 1 \& 1 STEP 1 UNTIL J DO
BEGIN
IF F[I] IS ATOM THEN D[I] ↔IF F{I]=X THEN 1 ELSE O ELSE
BEGIN
IF F[l] = F[J+1]: OF(ANY) |T| F(J+2]:OF (ANY), THEN
GO TO L[K] ELSE GO TO ERROR;
END;
GO TO CONTINUE;
L1:D[1] - D. [J+1] + D. [J+2]; 60 TO NEXT;
L2: D[1] ~ D.[J+1] - D.[J+2]; GO TO NEXT;
L3: D[1] - D.[J+1]*F[J+2] + D.[J+2]*F[J+1]; 60 T0 NEXT;
L4: D[1] \& (F[J+2]*0. [J+1]-F[J+1]*0.[J+2])/F[J+2]+2; GO TO NEXT;
L5: D[1] FF[J+2]*F{J+1]t(F(J+2) - 1) +LN(F[J+1])*F[I]*D.[J+2);
NEXT: J J J 2;
CONTINUE: ;
END OF LOOP:
FOR 1 \& J STEP -1 UNTIL 1 DO
D[I] \& EVAL D[I];
DERV \& D[1];
END PROCEDURE;

```

FORmULA PROCEDURE TO COMPUTE THE GENERAL TAYLOR SERIES EXPANSION OF A FORMULA WITH RESPECT TO
\(N\) variables
```

FORM PROCEDURE TAYLOR(F,U,V,M,N);
FORM F; SYMBOL U,V; INTEGER M,N;
COMMENT: LET F BE THE FORMULA}\mathrm{ TO BE EXPANOEO, LET U BE A SET OF INITIAL
VALUES, LET V BE A SET OF VARIABLES IN F\& X1,X2,···..,ETC.., LET M
BE THE NUMBER OF TERMS DESIRED, AND LET N BE THE NUMBER OF VARIABLES
IN F.
BEGIN SYMBOL W,S,R; FORM Z;G; FORM ARRAY T,H[1\&N]; INTEGER I,J;
FOR 1 \& 1 STEP 1 UNTIL N DO BEGIN
INSERT I TH OF V - I TH OF U AFTER LAST OF <|>%;
INSERT H.[I] AFTER LAST OF <S>;
INSERT T.[l] AFTER LAST OF <R>i END;
Z- EVAL(<V>)F(\&R>); FACT \& 1;
TAYLOR \leftarrowEVAL(<R>)Z (<U>);
FOR I \& 1 STEP 1 UNTIL M DO BEGIN
G-0; FACT - FACT*I ;END;
FOR J\&1 STEP 1 UNTIL N DO
BEGIN G\leftarrowG + H.[J]*DERV(Z,T.[J]); 2-G; END;
TAYLOR \leftarrowTAYLOR + EVAL( < <>, <R>)Z (<|>>,<\gamma>)/FACT;
END PROCEDURE;

```

BEGIN
COMMENT: THIS PROGRAM FINDS THE MINIMUM PATH AND PRINTS THIS PATH TOGETHER WITH ITS LENGTH. THE GRAPH IS ENTERED AS A SET OF NODES WITH DESCRIPTION LISTS ATTACHED TELLING THE OTHER NODES TO WHICH EACH NODE IS IMMEDIATELY CONNECTED (ATTRIBUTES) AND TELLING THE LENGTHS OF THE EDGES THAT FORM THOSE CONNECTIONS (VALUES). FURTHER, AN INDEX IS ATTACHED TO EACH NOOE WHICH IS ZERO FOR THE ORIGIN and a number greater than the sum of all edge lengths in the GRAPH FOR THE OTHER NODES. AN ALGORITHM, GIVEN IN BERGE "GRAPH THEORY' IS USED WHEREBY IF INDEX[A] IS THE INDEX OF NODE A, IF L[A,B] IS THE LENGTH OF THE EDGE FROM A 10 B, AND IF
INDEX[A] + L[A,B] < INDEX[B] THEN THE INDEX OF B IS REPLACED BY THE NUMBER INDEX[A] + L[A,B] AND THIS PROCESS IS CONTINUED UNTIL NO NODE HAS AN INDEX THÁT CAN BE FURTHER DIMINISHED. THE INDEX OF THE TERMINUS HAS THEN BEEN DECREASED MONOTONICALLY AND THERE MUST HAVE BEEN A NODE LAST USED FOR THIS PURPOSE. THIS IS THE SECOND TO LAST NODE IN THE MINIMUM PATH. LIKEWISE, THE index of the second to last node has been decreased monotonically and there must have been some node last used for this purpose. this is the third to last node in the minimum path. iterating we FIND THE MINIMUM PATH CONNECTING THE ORIGIN TO THE TERMINUS [ FOR A PROOF SE E BERGE, OP .CIT.]. HERE WE TAKE AS AN EXAMPLE THE FOLLOWING GRAPH WITH ORIGIN AO AND TERMINUS A5;

RE


REAL N; SYMBOL AO,A1,A2,A3,A4,A5,I NDEX,LASTNODE, NODELIST,MINPATH,S,T; BOOLEAN ITERATE; LABEL AGA N,ALPHA,BYPASS;
```

NODELIST - [ A0,A1,A2,A3,A4,A5];
AO \leftarrow / [ A1:1][Á2:2][Á3:7][A44:3][INDEX:0];
AK- / [ AO:1][A2:1][A3:3][1NDEX:100];
A2 \leftarrow / [ A0:2][A1:1][A3:1][A4:2][A5:6][INDEX:100];
AB \leftarrow/ [ A1:1][A2:1][A5:2][INDEX:100];
A4\leftarrow/[{AO:3][A2:2][A5:3][INDEX: 100];
A5 \leftarrow/ [ A3:2][A2:6][A4:3][INDEX:100];
AGAIN: ITERATE \&FALSE;
FOR S \& ELEMENTS OF <NODELIST> DO
FOR T\&ATTRIBUTES OF <<> DO
BEGIN
IF <T> = INDEX ~ <T> = LASTNODE THEN GO TO BYPASS;
N \& THE INDEX OF <T> + THE <T> OF <S> ;
IF N < THE INDEX OF < < THEN
BEGIN
ITERATE \& TRUE; THE INDEX OF <S> IS N;
THE LASTNODE OF <S> IS <T> ;
END;
BYPASS: ;
END FOR LOOP;
If ITERATE = TRUE THEN GO TO AGAIN;
COMMENT: HERE WE PRINT THE RESULTS:

```
40.

PRINT( <'THE LENGTH OF THE MINIMUM PATH \(\mid S^{\circ}>\) );
\(\mathrm{N}-\mathrm{THE}\) INDEX OF A5;
NAME (A5); PRINT( < 2R,1D>);
MINPATH \(-\{A 0, A 5]\);
\(X \leftarrow A 5 ;\)
ALPHA: IF THE LASTNODE OF <X> \(\neg=\) NIL THEN
BEGIN INSERT THE LASTNODE OF <X> 1ST BEFORE LAST OF < IINPATH>; \(X \leftarrow\) THE LASTNODE OF \(<X>; 60\) TO ALPHA; END
PRINT ( <E>, <'THE MINPATH IS \({ }^{\circ}>\) )
MAME (MINPATH); PRINT( < E, ILIST>);
END PROGRAM

BEGIN
COMMENT: ASSUME THAT WE ARE GIVEN A CLASS OF EXPRESSIONS DEFINED BY THE FOLLOWING BACKUS NORMAL FORM SYNTAX EQUATIONS.
```

<ARITHMETIC EXPRESSION> ::= <TERM> | <t> < TERM> | <ARITHMETIC EXPRESSION>
<t-> < TERM >
< TERM > ::= <FACTOR> | <TERM> < */ > <ACTOR >
< FACTOR > ::= <PRIMARY > | \&ACTOR> \uparrow <PRIMARY>
< PRIMARY > ::= < IDENTIFIER > 1 ( AARITHMETIC EXPRESSION>)

```

解 ARE TO TRANSLATE THIS CLASS OF EXPRESSIONS INTO CORRESPONDING INFIX EXPRESSIONS IN THE CLASS DEFINED BY THE FOLLOWING BACKUS NORMAL FORM EQUATIONS.
```

< PREFIXA E > : := < TERM > | NEG < TERM > | <+> <PREFIXA E > < TERM >
< TERM > ::= < FACTOR > | < */ > < TERM > < FACTOR >
< FACTOR > ::=< <PRIMARY > | t < FACTOR > < PRIMARY >
< PRIMARY > s:= < IDENTIFIER > | < PREFIXA E >

```

HERE NEG IS A UNARY NEGATION OPERATOR. WE SEE THAT A UNARY MINUS PRECEDING A TERM IN AN INFIX EXPRESSION IS PERMITTEO AND MUST BE TRANSLATED INTO THE PREFIX UNARY OPERATOR NEG FOLLOWED BY THE TERM. THUS THE EXPRESSION - \((A+B) * C \uparrow 2+E * D\) HOULD BE TRANSLATED AS + NEG \(*+\) A B + C \(2 * E\). THE PROGRAM FIRST READS A SOURCE STRING TO BE TRANSLATED AND STORES THIS EXPRESSION ITEM BY ITEM IN A LIST FOUND AS THE CONTENTS OF THE SYMBOL "INPUT". A SIMULATION OF A FLOYD-EVANS PRODUCTION TRANSLATOR IS THEN USED TO ACCOMPLISH THE TRANSLATION;
```

SYMBOL S,STACK,INPUT,X,L1,L2,L3,U,V,H,Y,PM,TD,IDENT,LFTPAREN,P,F,T,AE;

```
LABEL AEO,AE1,P1,F1,T1;
PROCEDURE REVERSE; SYMBOL Q;
    BEGIN Q * < STACK > ; T STACK; INSERT \&Q> AFTER LAST OF <STACK> END;
PROCEDURE SCAN;
COMMENT: THIS PROCEDURE SCANS THE NEXT CHARACTER FROM THE LIST STORED IN THE
CONTENTS OF THE SYMBOL "INPUT" AND STACKS IT LAST IN THE WORKSPACE S;
    BEGIN INSERT 1ST OF <INPUT> AFTER LAST OF \(\leqslant>\); DELETE IST OF <INPUT>;\&END;
PROCEDURE APPENDOPERA TOR;
    BEGIN INSERT <X> BEFORE 1ST OF <STACK>; END;
OMMENT: CLASS DEFINITIONS;
    L1 \(\leftarrow[+,-1\);
    LET (|PM|) \(=\{\) U| AMONG(U,L1) \(]\);
    L2 - [ *, / ];
    LET (|TD|) = [V| AMONG(V,L2) ];
    LET \((|I D E N T|)=[W|<W>| S ~ S Y M B O L ~] ;\)
    LET (|LFTPAREN|) \(=\left[Y \mid\langle\gamma\rangle={ }^{\prime}{ }^{\prime}\right]\);
42.

COMMENT: HERE WE READ AND STORE THE EXPRESSION TO BE TRANSLATED INTO THE CONTENTS OF THE SYMBOL INPUT. THE CONTENTS OF INPUT ARE READ OFF CONSECUTIVELY ELEMENT BY ELEMENT EACH TIME THE PROCEDURE SCAN IS CALLED DURING THE PROGRAM:
MAME (INPUT); \(\operatorname{READ}(<E>,<1\) LIST > ) ;
SCAN; COMMENT: INITIALLY WE START THE TRANSLATION BY SCANNING THE FIRST
CHARACTER IN THE INPUT STRING;
GO TO AEO;
COMMENT: ENTER THE TRANSLATOR;
AEO: IF LAST OF \(\langle>\) IN (|PM|) THEN SCAN AND GO TO AEO;
IF LAST OF \(\delta>\) IN (|IDENT|) THEN BEGIN
LSTACK; STACK - LAST OF \(<S>\);
DELETE LAST OF <S>; INSERT P AFTER LAST OF \(\langle>\); SCAN; GO TO AEO; END;
IF LAST OF <S> IN (|LFTPAREN|) THEN SCAN AND GO TO AEO ELSE GO TO ERROR;
P1: IF LAST 4 OF <S> HAS F,X:T,P,\$1 THEN BEGIN REVERSE; APPENDOPERA TOR;
DELETE BETWEEN 3RD BEFORE LAST AND LAST OF <S>; GO TO F1;END;
IF LAST 2 OF <S> HAS P,\$1 THEN DELETE 1ST BEFORE LAST OF \(\mathrm{S}>\) AND INSERT F 1ST BEFORE LAST OF <S> AND GO TO F1 ELSE GO TO ERROR;
F1: IF LAST 2 OF \(<S>\) HAS F, \(\uparrow\) THEN SCAN ANO GO TO AEO;
IF LAST 4 OF < \(\gg\) HAS \(T, X:\) (|TD|), F, \$1 THEN BEGIN REVERSE;APPENDOPERATOR; DELETE BETWEEN BRD BEFORE LAST AND LAST OF \(<S>\); GO TO T1; END;
IF LAST 2 OF \(\langle>\) HAS \(F, \$ 1\) THEN DELETE 1ST BEFORE LAST OF \(<>\)
AND INSERT T 1ST BEFORE LAST OF \(\rangle\) AND GO TO T1 ELSE GO TO ERROR;
T1: IF LAST 2 OF <S> HAS T, (|TD|) THEN SCAN AND GO TO AEO; IF LAST 4 OF \(\langle>\) HAS AE, X: (|PM|),T, \(\$ 1\) THEN BEGIN

REVERSE; APPENDOPERATOR; DELETE BETWEEN 3RD BEFORE LAST AND LAST OF <S>; GO TO AE1; END;
IF LAST 3 OF <S> HAS X:(|PM|),T,\$1 THEN BEGIN
If <x> = "-" THEN \(X \leftrightarrow N E G ;\) APPENDOPERATOR;
DELETE BETVEEN 3RD BEFORE LAST AND LAST OF \(\ll>3\)
INSERT AE 1ST BEFORE LAST OF \(\angle S>\); 60 TO AE1; ENO;
IF LAST 2 OF 《S> HAS T, \$1, THEN DELETE IST BEFORE LAST IN 《S>
AND INSERT AE \(1 S^{\prime} T\) BÉFORE LAST IN \(\langle>\) AND GO TO AEI ELSE GO TO ERROR;
AE1: IF LAST 3 OF \(\langle>\) HAS (, AE, ) THEN DELETE LAST 3 OF \(\langle>\) AND
AND INSERT P 1ST AFTER LAST OF <S> AND SCAN AND GO TO P1;
IF LAST 2 OF \(\leqslant>\) HAS AE, (|PM|) THEN SCAN AND GO TO AEO; IF LAST 2 OF <S> HAS AE, \(\$ 1\) THEN GO TO EXIT ELSE GO TO ERROR

GRROR: PRINT(<'ERRONEOUS SOURCE STRING*,E>);
EXIT: \(\operatorname{NAME}(\langle T A C K>)\); \(\operatorname{PRINT}(<E>,<1 L I S T>,<E>)\);
END OF PROGRAM;
\(-(A+B) * C \uparrow 2+E * D ;\) COMMENT: \(\leftarrow\) INPUTTEXT;
EXPECTED OUTPUT IS + NEG * + AB+C \(2 * E D\) -

NOTE: THE WORD " AND" HAS BEEN USED IN PLACE OF ; IN THE ABOVE TEXT TO
CONCATENATE SEVERAL STATEMENTS INTO A COMPOUND STÁTEMENT WITHOUT THE USE
OF THE BRACKETS BEGI N--END.

BEGIN
COMMENT: THIS ALGORITHM OF HAO WANG [CF.IBM JOURNAL, JAN *60,PP 2-22] DETERMINES THE VALIDITY OF WELL FORMED FORMULAS OF PROPOSITIONÁL CALCULUS. THE FORMULA TO BE PROVED OR DISPROVED ENTERS AS A LIST CONSISTING OF THE MARK \(\rightarrow\), FOLLOWED BY THE FORMULA (EXPRESSED IN FORMULA ALGOL AS A BOOLEAN FORMULA), FOLLOWED BY AN OCCURRENCE OF THE SYMBOL NIL. THIS LIST IS STORED AS THE CONTENTS OF THE SYMBOL SEQUENT. WE SEARCH FOR THE FIRST LOGICAL CONNECTIVE IN THE SEQUENT. IF THERE IS NONE WE TRANSFER TO RULEO WHICH DETERMINES THE VALIDITY OF THE FORMULA ACCORDING TO A TERMINAL RULE GIVEN BY WANG. IF THERE WAS A LOGICAL CONNECTIVE, THEN, HAVING NOTED THE POSI TION OF THE ARROW \(\rightarrow\) (ALL THAT IS NECESSARY IS TO KNOW WHE THER THE ARROW CAME BEFORE THE FIRST LOGICAL CONNECTIVE), WE TRANSFER TO THE APPROPRIATE RULE TO TRANSFORM THE SEQUENT IN ORDER TO ELIMINATE THE LOGICAL CONNECTIVE. IF THE RULE SELECTED PRODUCES TWO SEQUENTS AS A RESULT OF ELIMINATING THE CONNECTIVE, ONE OF THEM IS ENTERED INTO the SECOND LEVEL OF THE PUSH DOWN STACK CONTAINED IN THE SYMBOL SEQUENT. THE OTHER IS PLACED ON THE TOP LEVEL AND IS PROCESSED NORMALLY. AFTER THE TOP LEVEL HAS BEEN PROCESSED THE LOWER LEVELS ARE PROCESSED PROVIDED THE PROCESS HAS NOT BEEN HALTED BY THE DISCOVERY OF AN INVALID SEQUENT. THE ALGORITHM STOPS EI THER WHEN AN INVALID SEQUENT HAS bEEN FOUND OR WHEN, ALL SEQUENTS HAVING BEEN SHOWN VALID, THE PUSH DOWN STACK IS EMPTY.

FORMULA A,B,F; SYMBOL SEQUENT T,P,Q,I; INTEGER N,ARROWPOSITION;BOOLEAN VALID; LABEL ITERATE,AGAIN,RULEO,RULE1,RULE2,RULE 3,RULE 4 ,RULE5,RULE \(6, R U L E 7, R U L E 8\), RULE9,RULE 10,TEST1,HALT; SWI TCH SWI TCH1ヶRULE1,RULE2 ,RULE3,RULE4,RULE5, RULE6,RULE7,RULE8,RULE9,RULE10;

PROCEDLRE EXTRACTMAINOP ( \(G, S\) ); FORMULA \(G\); SYMBOL \(S\);
COMMENT: THIS PROCEDURE FINDS THE MAIN OPERATOR OF THE BOOLEAN FORMULA G AND STORES THIS OPERATOR IN THE CONTENTS OF THE SYMBOL S. IT ALSO EXTRACTS THE LEFT AND RIGHT HAND SUBEXPRESSIONS, IF ANY, AND STORES THEM IN A AND B RESPECTIVELY;

BEGIN
IF \(G==\) ATOM THEN \(S \leftarrow\) NIL ELSE
IF \(G==\rightarrow A: O F(F O R M)\) THEN \(S \leftarrow{ }^{\circ} \overbrace{}^{\circ}\) ELSE
IF \(G==A: O F(F O R M) \sim B: O F(F O R M)\) THEN \(S \leftarrow{ }^{\circ} \wedge^{\circ}\) ELSE
IF \(G=A: O F(F O R M) \vee B: O F(F O R M)\) THEN \(S \leftarrow \cdots\) ELSE
IF \(G=A: O F(F O R M)\) EQL \(B: O F(F O R M)\) THEN \(S \leftarrow{ }^{\circ} E Q L\) ' ELSE
IF \(G=A: O F(F O R M)\) IMP \(B: O F(F O R M)\) THEN \(S \leftarrow \bullet I M P\). ELSE
PRINT( <'ERROR MALFORMED EXPRESSION',E>);
END PROCEDURE;
INTEGER PROCEDURE WHICHRULE; SYMBOL L; INTEGER K; LABEL ALPHA; BEGIN

COMMENT: THIS PROCEDURE DETERMINES AN INTEGER TELLING WHICH RULE TO TRANSFER TO DEPENDING ON THE LOGICAL CONNECTIVE GIVEN AND WHETHER IT OCCURRED BEFORE OR AFTER THE ARROW \(\rightarrow\);
\(L \leftarrow[\neg, \wedge, \vee, I M P, E Q L]\);
FOR K \(\leftarrow 1\) STEP 1 UNTIL 5 DO
IF K TH OF \(\rangle=\langle\delta\rangle\) THEN GO TO ALPHA;
ALPHA: WHICHRULE \(\leftarrow 2 * K\) - ARROWPOSITION;
END PROCEDURE;
44.

BEGIN
SEQUENT> \(-[\) < SEQUENT>,NIL];
ITERATE: N-1; ARROWPOSITION \(\leftarrow 0\); NAME (SEQUENT);PRINT(<1LIST,E>);
AGAIN: IF N TH OF SEQUENT \(>={ }^{\prime} \rightarrow{ }^{\prime}\) THEN BEGIN ARROWPOSITION \(\leftarrow 1 ;\) N-N+1; GO TO AGAIN; END ELSE IF \(N\) TH OF SEQUENT \(=\) NIL THEN GO TO RULEO ELSE \(F \leftarrow N\) TH OF <SEQUENT>; EXTRACTMAINOP \((F, T)\); IF \(<T\rangle=\) NIL THEN BEGIN \(N-N+1\); GO TO AGAIN; END ELSE GO TO SWI TCH1(WHICHRULE);

RULE 1: DELETE N TH OF < SEQUENT>; INSERT A BEFORE IST OF <SEQUENT>; GO TO ITERATE;
RULE2: DELETE N TH OF SEQUENT>; INSERT A AFTER LAST OF \(\langle E Q U E N T>;\) GO TO ITERATE;
RULE3: DELETE N TH OF <SEQUENT>; Q--SEQUENT>; INSERT A AFTER (N-1)ST OF <SEQUENT>; \(\downarrow\) SEQUENT; SEQUENT \(\leftarrow<Q>;\) INSERT B AFTER (N-1)ST OF < SEQUENT>; GO TO ITERATE;
RULE4: DELETE N TH OF SSEQUENT>; INSERT A AFTER (N-1)ST OF <SEQUENT>; INSERT B AFTER N TH OF <SEQUENT>; GO TO ITERATE;
RULE5: COMMENT: SAME AS RULE 4; GO TO RULE4;
RULE6: COMMENT: SAME AS RULE 3; GO TO RULE3;
RULE 7: DELETE N TH OF <SEQUENT>; INSERT A IST BEFORE 1ST ' \(\rightarrow\) ' OF SEQUENT>; INSERT B AFTER N TH OF <SEQUENT>; GO TO ITERATE;
RULE8: DELETE N TH OF <SEQUENT>; Q \& SÉQUENT>; INSERTA AFTER LAST OF SEQUENT>; \(\downarrow\) SEQUENT; SEQUENT-\& \(>\); INSERT B AFTER (N-1)ST OF <SEQUENT>; GO TO ITERATE;
RULE9: DELETE NTH OF <SEQUENT>; QQ- SSEQUENT>; INSERT B BEFORE 1ST OF <SEQUENT>; INSERT A AFTER NTH OF <SEQUENT>; LSEQUENT; SEQUENTH-Q>;
INSERT A BEFORE 1ST OF <SEQUENT>; INSERT B AFTER N TH OF <SEQUENT>; GO TO ITERATE:
RULE10:DELETE N TH OF <SEQUENT>; Q \(\propto\) <SEQUENT>; INSERT A, B AFTER LAST OF <SEQUENT>; LSEQUENT; SEQUENT-\&Q>; INSERT A,B BEFORE 1ST OF <SEQUENT>; GO TO ITERATE;

COMMENT: RULEO CHECKS TO SEE IF SOME ATOM ON THE RIGHT is also ON the left IN THE SEQUENT;
```

RULEO: IF <SEQUENT> HAS P:$,->,Q:$ THEN GO TO TEST1 ELSE PRINT(<'ERROR
MALFORMED SEQUENT',E>);
TEST1: VALID ↔FALSE;
FOR 1 \& ELEMENTS OF <P> DO
IF AMONG(<1>,Q) THEN VALID \& TRUE;
NAME(SEQUENT); PRINT(<1LIST,E>);
IF VALID = FALSE THEN BEGIN PRINT(<'THEOREM NOT VALID',E>);
GO TO HALT;END;
TSEQUENT; IF - EMPTY(SEQUENT) THEN GO TO ITERATE ELSE
PRINT(<'THEOREM VALID',E>);
HALT:
;
END PROGRAM;

```
IV. THE BACKUS NORMAL FORM SYNTAX FOR FORMULA ALGOL
```

Add to the Revised Algol Report:
<formula expression> ::= <arithmetic expression>|<Boolean expression>|
<an arithmetic expression (Boolean expression) in which some
of the primaries (Boolean primaries) have been replaced
by "procedure formula", "array formula", or "eval formula">|
<substitution formula>
<conditional formula> ::= .TF <formula expression> THEN <expression>
ELSE <expression>
<procedure formula> ::= <function designator>.<actual parameter part>
<assignment formula> ::= . \leftarrow<expression>
<array formula> ::= <identifier> . [<subscript list>]
<eval formula> ::= EVAL_L_variable> | EVAL <bound variables>
<expression> <list of values>
<list of values> : := (<actual parameter 1ist>) | ([<variable>])
<bound variables> ::= (<variable list>) | ([<variable>])
<variable list> ::= <variable> | <variable 1ist>, <variable>
<expression> : := <arithmetic expression> | <Boolean expression> |
<designational expression> | <formula expression> |
<pattern expression> | <symbolic expression> |
<tree expression>
<unlabelled pattern primary> ::= <type> | OF (<variable>) | ATOM

```
```

4 6 .
<pattern primary> ::= <unlabelled pattern primary> |
<variable> : <unlabelled pattern primary>
<pattern structure> ::= <a formula expression in which some of the
primaries may have been replaced by pattern primaries and
some of the operators may have been replaced by
|<variable>|>
<pattern> ::= <formula expression> == <pattern structure>
<identifier> ::<formula expression> >>
<identifier> :: <pattern expression> |
<formula expression> >> <pattern structure>
<variable> ::= <simple variable> | <subscript variable> |
.<identifier>

```
```

<symbolic expression> ::= <variable> | <function designator>|
<selection expression> | <value retrieval expression>|
'<' <symbolic expression> '>'
<list valued symbolic expression> ::= <symbolic expression>
having a list of symbols as value.

```

In the following syntax equations the syntactic class <symbolic expression> refers to that subclass of symbolic expressions, as defined above, which have single values. The syntactic class <list valued symbolic expression> refers to that class of symbolic expressions, as defined above, which have lists of symbols as values.
<symbolic expression 1ist> : := <symbolic expression> |
<symbolic expression list>, <symbolic expression>
<tree expression> : \(:=\) <tree expression list>]
<tree expression list element> ::=<expression> |
[<tree expression list element>] <description list> |
<symbolic expression> <description list> |
<tree expression list> ::=<tree expression list>,
<tree expression list element> |
<tree expression list element>
<description list> : := / <attribute value list>
<attribute value list> ::=<attribute value segment> |
<attribute value list> <attribute value segment>
<attribute value segment> ::=
[<symbolic expression> : <expression 1ist>]
<value retrieval expression> ::= THE <symbolic expression>
OF <symbolic expression>
48.
```

<value entry statement> ::= THE <symbolic expression> OF
<symbolic expression> <is phrase> <expression>
<is phrase> ::= IS | IS NOT | IS AlSO
<list pattern> ::= <list valued symbolic expression> = =
[<constituent selector list>] |
<list valued symbolic expression> ==
<list valued symbolic expression> | <symbolic expression> = =
<symbolic expression>
<constituent selector 1ist> ::= <constituent selector> |
<constituent selector list>, <constituent selector>
<constituent selector> ::= \$ | \$ <unsigned integer> |
<class name> | <symbolic expression> | <augmented type>
<list valued symbolic expression> |
<symbolic expression> <description list> |
<label> : <constituent selector>
<class name> ::= (| <symbolic expression> |)
<class primary> ::= <class name> | [<class expression>]
<class secondary> ::= <class primary> | ᄀ <class primary>
<class factor> ::= <class secondary> | <class factor> ^
<class secondary>
<class expression> ::= <class factor> | <class expression> V
<class factor>
<class definition> ::= LET <class name> = [<formal parameter> '|'
<Boolean expression> ] | LET <class name> =
<class expression>

```
```

    49.
    <assignment statement> ::= <symbolic expression> \leftarrow<description 11st>|
<symbolic expression> \leftarrow<expression>|
<symbolic expression> \leftarrow<tree expression list>
<for 1ist element> ::= ... | <symbolic expression>|
ELEMENTS OF <list valued symbolic expression> |
ATTRIBUTES OF <symbolic expression>
<for clause> ::= ...| FOR <symbolic expression> \leftarrow<for 11st> DO |
PARALLEL FOR [<formal parameter list>] }
ELEMENTS OF [<symbolic expression 11st>] DO |
PARALLEL FOR <list valued symbolic expression> }
ELEMENTS OF <list valued symbolic expression> DO
<unlabelled basic statement> ::= ... | <class definition> |
<value entry statement> | <push down statement> |
<pop up statement> | <editing statement>
<push down operator> ::= \downarrow | <push down operator> \downarrow
<pop up operator> ::= \uparrow | <pop up operator> 1
<push down statement> ::= <push down operator> <symbolic expression>
<pop up statement> ::= <pop up operator> <symbolic expression>
<relation> ::= ... |<symbolic expression> = = <class name> |
<symbolic expression> =<symbolic expression> |
<list valued symbolic expression> =
<list valued symbolic expression> | <list pattern>
<augmented type> ::= REAL | INTEGER | BOOLEAN | FORMULA
SYMBOL | SUBLIST | LOGIC | HALF | TEXT | ATOM |

```
```

5 0 .
<selection expression> ::= <selector> OF
<list valued symbolic expression>
<ordinal suffix> ::= ST | ND | RD | TH
<ordinal selector> ::= <arithmetic primary>
FIRST | LAST
<elementary position> ::= <ordinal selector> | <ordinal selector>
<class name> | <ordinal selector> <expression> |
<ordinal selector> <augmented type>
<position> ::= <elementary position> | <arithmetic primary>,
<ordinal suffix> BEFORE <elementary position> |
<arithmetic primary>u<ordinal suffix> AFTER
<elementary position>
<selector> : := BETWEEN <position> AND <position> |
ALL AFTER <position> | ALL BEFORE <position> |
FIRST <unsigned integer> | LAST <unsigned integer> |
<position> | ALL <expression> | ALL <augmented type> |
ALL <c1ass name> |
<insertion locator> ::= BEFORE <position> OF |
AFTER <position> OF
<insertion locator list> ::= <insertion locator> |
<insertion locator list>, <insertion locator>
<insertion locator part> ::= <insertion locator> |
(<insertion locator list>)

```
```

<selector 1ist> : := <selector> | <selector 1ist>, <selector>
<selector part> ::= <selector> | (<selector list>)
<editing statement> ::= INSERT <tree expression list>
<insertion locator part> <list valued symbolic expression>|
DELETE <selector part> OF <list valued symbolic expression>|
ALTER <selector part> OF <list valued symbolic expression>
TO <expression> | DELETE <symbolic expression>
<expression> ::= ... | <arithmetic expression> | <Boolean expression>|
<designational expression> | <formula expression>|
<symbolic expression> | <tree expression>|
<pattern expression>

```
<expression list> : := <expression> |<expression 1ist>, <expression>
1. Gelernter, H., Hansen, R.R., Gerberich, C.L.: "A Fortran compiler List processing Language", Journal ACM, ㄱ, 87 - 101 (Apri1 1960).
2. Bond, E., et al: "FORMAC, An Experimental Formula Manipulation Compiler", Proc 19th National Conference ACM 1964, K2-1.
3. Brown, W.S., "The ALPAK System for Non-numerical Algebra on a Digital Computer", Bell Telephone Laboratories, Inc., Murray Hill, New Jersey, internal publication.
4. Perlis, A.J., and Iturriaga, R.: "An Extension to Algol for Manipulating Formulae', Communications of the ACM, 7, 127-130, (February 1964).
5. Christensen, Carlos: "AMBIT, A Programming Language for Algebraic Symbol Manipulation", Paper CA-64-4-R, Computer Associates, Inc., Wakefield, Massachusetts.

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This manual is a reference guide for MTHAT. As reference material, the various features of MTHAT are organized by their functions. An alphabetical listing of sudos is also included.

This manual is designed to be used in coordination with:
Bendix G-20 Central Processor Machine Language Manual, available through Control Data Corporation.

The following papers are also needed as references for the Assembly Language Code on the Carnegie Tech, CDC G-21. The papers may be obtained by writing to the Documentation Office, PH118-P, Department of Computer Sciences, Carnegie Institute of Technology, Pittsburgh, Pa., 15217.
"Specifications for the Use of Routines in the Carnegie Tech Monitor 'THEM THINGS'", code COO-42.1 (The 'THEM THINGS' write-up is also included in the 1965 User Manual, page 291.)
"Monitor References for Staff Members", code CID. 47
"Execute OPCODE" (December 11, 1963)
"Scatter Repeat and Indirect Block-Length Addressing" (January 15, 1964)
"Special Registers" (March 26, 1964)
"CC-11" (March 30, 1964)

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1. Introduction
2. Input cards
3. Card format
4. Input parameters
5. Regions, labels, and free names
6. G-21 instructions
7. Controlling the assembly listing
8. Leaving MTHAT to execute assembled code
9. Controlling region and label definitions
10. Assembling G-21 instructions
11. Assembling integers, addresses, and Boolean data
12. Assembling floating point numeric data
13. Assembling alphanumeric data
14. Altering the location or contents of assembly
15. Concordance
16. Free names
17. Macros
18. Error detection and correction
19. Assembly-time iteration
20. Parallel tables
21. Controlling input cards
22. Saving assembled code
23. User-declared sudos
24. Run-time features
25. Control console interaction
26. Hardware registers and line commands
27. Other sudos
28. List of G-21 instructions and standard modes
29. List of alphanumeric characters
30. List of G-21 shift multipliers
31. Octal-decimal conversion tables
32. Index of sudos
33. List of predefined labels

\section*{MTHAT}
1. INTRODUCTION
MTHAT is a one-pass symbolic assembler for the CDC (formerly
Bendix) G-21 computer. It is designed to be used in conjunction with
the Carnegie Tech G-2l monitor system.
The input to MTHAT is a set of punched cards, or the images of
punched cards obtained from either the G-2l control console or the
remote teletype units. The outputs are G-21 machine code in the
computer memory, uaually one word of code for each card input, and a
printed assembly listing. There also are provisions for communication
between mTHAT and an operator or programmer at the G-2l control console.
mTHAT is called a one-pass assembler because usually each input
card is processed once only.
2. INPUT CARDS

The input cards or card images to MTHAT may be classified into four categories.
1. Cards to be listed only. The images of these cards are printed on the assembly listing, but the cards are otherwise ignored by MTHAT. For more details, see the LIS sudo.
2. G-21 instruction words. MTHAT translates the card images into the proper machine code, and stores the code in the computer memory for execution after the MTHAT assembly has been completed.
3. MTHAT pseudo-instructions, called "sudos." These sudos are executed immediately by the MTHAT system. However, some of them result in the storage of G-21 machine code, for use after the MTHAT assembly has been completed.
4. MIHAT macro-instructions. The appearance of a single macro card may result in the assembly of several other cards. The choice of which other cards are assembled is determined by the user when he writes the macro declaration. More details appear in the discussion of macros.

\section*{3. CARD FORMAT}


Columns 24 to 67: Parameters field. The parameters appropriate to the opcode appear here. The parameters are separated by commas, and terminated by a semicolon. Everything to the right of the semicolon is treated as comments. If a semicolon is used to terminate the parameters before the specified number of parameters have been supplied, then the remaining parameters are treated as blanks. Blank parameters are interpreted as zeroes, unless specified otherwise.

All other columns: Immaterial
Some opcodes do not use all the fields listed above. Also, some opcodes use other fields which are not listed above. All opcodes use the label and opcode fields. Those opcodes which require parameters use the parameters field, unless specified otherwise. The other fields are used only where specified.

MTHAT processes cards by sranning first the label field, then the opcode field, then the other fields as appropriate. Thus the label field is processed even on cards which do not cause the assembly of G-21 code, such as COM sudo cards.

\section*{4. INPUT PARAMETERS}

Unless specified otherwise, parameters are expressions consisting of constants and variables, and operators on the constants and variables. The types of constants are as follows:
1. Blank. Blank parameters are interpreted as zeroes, unless specified otherwise.
2. Decimal integer. One or more decimal digits.
3. Octal integer. A slash, /, followed by one or more octal digits.
4. Power of 2. A dollar sign, \(\$\), followed by a decimal integer. The allowable range is from \(\$ 0=1\) to \(\$ 31=/ 20000000000\).
5. The numeric value of alphanumeric characters. A greater than, \(>\), followed by 4 characters in the next 4 columns of the card. The internal representations of the characters (See Section 29) are concatenated in the standard 4-character-per-word, 8-bit format. The value of the constant is taken to be the value of the resulting 32 -bit integer. Blank characters in the specified 4 columns are significant. If the 4 columns would extend past the end of the field on the card, the trailing characters are treated as blanks.
6. The contents at assembly time of a specified location. An expression whose value equals the desired address is surrounded by parentheses or by square brackets. If surrounded by parentheses, a numeric access is made of the named location. If surrounded by brackets, a logic access is made of the named location. It is not possible to nest sets of parentheses or brackets within each other.

\section*{The types of variables are as follows:}
7. Region. Described in Section 5.
8. Label. Described in Section 5.
9. Free name. Deacribed in Section 5.
10. Greater variable. There are six greater variables: \(A>, B>, C, D>, E>\), and \(F>\). They are used primarily as formal parameters for macros, although they may be used elsewhere if desired. They are described in Section 17.

The operators used in expressions are as follows:
+ add
- subtract
* multiply
: divide.... by convention, 0:0=0
\(\wedge\) Boolean bit intersection

The character \(V\) has a special use in both constants and variables, as described in Section 19. Blank spaces between nonblank characters forming a constant or variable are ignored completely, except in item 5 above.

Expressions are evaluated strictly from left to right, with no heirarchy among the operators. Thus \(1+2 * 3=9\), and 5: -7 produces an error because 5 is divided by 0 .

Expression evaluation is performed in double precision floating point arithmetic until a final value is obtained. The type of storage used for the final value depends upon the specific use of the parameter. If an integer is required, the floating point number is converted to an integer by truncation.

All the variables in an expression must have defined values at the time the expression is evaluated, unless specified otherwise.

Some sudos have listable parameters, or listable sets of parameters. Sudos with listable sets of parameters allow the parameters to be repeated several times on a single card, separated by commas. The action of the sudo is performed once for each set of parameters.

\section*{5. REGIONS, LABELS, AND FREE NAMES}

A region is a sequential area within the computer memory. The base of the region is the address of the first word in the region. If, for example, \(B\) is the name of a region, the \(B 15=B 0+15\).

A label is a name given to some particular location or value. The values of adjacent labels are not necessarily related. For example, if LO to \(L 20\) are 1 abels, it is possible for \(L 12=5\) and \(L 13=200\).

The syntax of regions and labels is the same for both: a letter or one of the other characters listed below (called "identifiers") followed by a decimal integer (called the "subscript"). If no subscript follows, then a subscript of 0 is assumed. The possible identifiers are:


Regions and labels are distinguished from each other by their first use in a program. If an identifier first appears in the label field of a card (See Section 3) or in a DEF sudo (See Section 9), then the identifier names a region. If the identifier first appears in a LBL sudo (See Section 9), then the identifier is used to name labels.

The identifier A is predefined by the MTHAT system to be a region, whose initial value is \(/ 30000\). A is used as the Current Location Counter for MTHAT; the value of A automatically is incremented by 1 for each word assembled.

Labels |0 to | 100 are predefined by MTHAT. Except for | 36 and \(\mid 37\), their values are the locations of subroutines and tables in the monitor. Labels ' 0 to ' 24 and | 36 and | 37 are predefined as the locations of subroutines and tables in MTHAT, or other references within MTHAT. A complete list is given in Section 33.

In some circumstances a label may be used whose value has not yet been defined at the time the card is processed. The use of undefined

\begin{abstract}
labels is described in detail where it applies. Regions mat always be defined before they are used. However, the use of regions is discouraged. No concordance is available for regions (See Section 15), and everything that can be done with regions can be done fust as well with labels. For example, the regional reference D10 could just as well be written D0+10, where D0 is a label.

Any combination of identifiers, digits, and the characters / \$ \(V\) which do not fit the syntax of constants or regions or labels may be used as a free name. The first 8 nonblank characters of a free name are significant; the remaining characters (if any) are ignored. Free names are put into a table (See Section 16) in the order in which they are encountered. The position of a free name in the table determines a subscript for the "period" identifier. For example, the 5th free name encountered is processed in exactly the same manner as though .5 had been written instead. If .0 to .200 have been declared as labels by the LBL sudo, and if the LFN sudo has been used, then 200 free names may be used instead of labels.

Regions and labels may be defined to have integer values between 0 and /177777 inclusive.
\end{abstract}

\section*{6. G-21 INSTRUCTIONS}

When a G-21 instruction is assembled, the opcode field of the card (See Section 3) may contain either the 3 characters of the opcode mnemonic (See Section 28) or the octal integer value of the opcode, with the slash (indicating an octal constant) omitted. For each G-21 instruction, MTHAT has defined a standard mode (See Section 28). If the opcode field contains a mnemonic and the mode field is blank, then the standard mode is assembled. Any punching in the mode field overrides the use of the standard mode. If the opcode field contains an octal integer, the standard mode always is 0 .

There are two parameters to an instruction. The first is the address, whose value must be between 0 and / 177777 inclusive. A single undefined label may be used for the address, if desired. When the value of the label is later defined, that value automatically will be stored in the instruction word that had the undefined label. No operators or constants or other variables may be used in the expression if an undefined label is used. The second parameter is the index, whose value must be between 0 and /77 inclusive. All variables used in the index expression must be defined when the card is processed.

The flag field is processed, but it is an error for a G-21 instruction to have a flag 1 or flag 3. A blank flag field is treated as flag 0.

If anything is punched in columns 22 or 23 of the card, then the G-21 internal representation of the characters in these two columns (See Section 29) is used as the address for the instruction word, and the index is set \(=0\). The parameters field of the card, where address and index usually are found, is ignored.

The G-21 instructions which use hardware registers or line comands are processed by MTHAT as special sudos; so that register mnemonics and line command mnemonics may be used. These instructions normally are of use only when programing a monitor system for the G-21.

The sudo ADC is processed like an OCA instruction, with standard mode \(=0\).

\section*{7. CONTROLLING THE ASSEMBLY LISTLNG}

The following sudos determine what is printed on the assembly listing, but do not affect the assembled code.

COM sudo - comment
no parameters
The contents of the card, except for the label field, are treated as comments only.

TOP sudo - type or print

2 parameters, nonlistable
If the first parameter \(:=0\), subsequent assembly continues with all printing of card images, octal dumps, etc., suppressed. If the first parameter \(=1\), subsequent assembly continues with all printing enabled. Initially MHAT has printing enabled.

The second parameter controls the printing of error messages, as follows:
\begin{tabular}{c|l} 
parameter value & error message appearance \\
\hline 0 & unchanged from previous state \\
\hline 1 & assembly listing only \\
\hline 2 & assembly listing and control console \\
\hline 3 & control console only
\end{tabular}

If an error message appears on the console, then a single card image is expected to be typed in by the operator at the control console to correct the error, before normal assembly resumes. The first TOP parameter does not affect the printing of error messages. Initially MIHAT error messages appear on the assembly listing only.

TOP card images always are printed.
```

LIN sudo - line

```
1 parameter, nonlistable

The printer is upspaced the designated number of blank lines. The LIN sudo card image never prints. A blank parameter is treated as LIN 1.

PAG sudo - page
no parameters

The printer is upspaced to the top of the next page before the card image is printed. Page titling and numbering initiated by the TOF sudo is turned off.

TOF sudo - top of form
alphanumeric string in columns 25 to 72
The printer is upspaced to the top of the next page. The TOF card image is not printed, but the string on the TOF card is printed as a page title at the top of this and subsequent pages. The pages are sequence numbered. This process is terminated by a PAG sudo or another TOF sudo.

LIS sudo - 11st
no parameters
The LIS card image is not printed. Columns 5 to 80 of subsequent card images are printed on the assembly listing, but are not processed by MTHAT in any other way. Listing terminates and normal processing resumes when a card is encountered with the single word THAT in columns 5 to 8. The THAT card image is not printed.

The LIS sudo terminates macro declarations in the same manner as the FIN sudo.
```

DMP sudo - octal dump
2 parameters, listable; mode
The firgt parameter is the starting location and the second
parameter is the ending location for an octal dump of the contents of
memory. The dump may start slightly before the specified starting
location, and may end slightly after the specified ending location.
Lines of dump which would contain all zeroes are not printed. A blank
line is printed after the dump.
The value of RXA is added to the specified starting and ending
locations, unless some nonblank character is punched in the mode field.
OCT sudo - octal listing
no parameters

```
    The value of \(A\) printed to the left of subsequent card images will
be in octal. Initially A is printed in octal.
DEC sudo - decimal listing
no parameters

The value of A printed to the left of subsequent card images will be in decimal.

PVE sudo - print value of expression
1 parameter, listable
The value of the parameter is printed. It is not an error if the parameter is a single undefined label. If the PVE card image came from
```

the control console, then the value of the parameter is typed back on
the console, as well as being printed on the assembly listing.

```
TIM sudo - time
no parameters
    The time is printed since the last occurrence of a TIM sudo, or
since the last job card if there were no preceding TIM sudos.
OPM sudo - operator message
no parameters

The standard monitor operator message is printed.

ERR sudo - errors

See Section 18.

\section*{8. LEAVING MTHAT TO EXBCUTE ASSEMBLED CODE}

OUF usually is used to terminate assembly. If MIHAT is retained in the computer memory after the end of an assembly, and is called again as a subroutine in the user's program, then either OUT or RET may be used to return control to the user's program. MTY usually is used to execute user-written subroutines during the course of assembly.

OUT sudo - leave MIHAT
1 parameter, nonlistable
Control is transferred to the location named. Before doing so, various assembly statistics are printed. This includes printing the concordance table, if one was generated (See Section 15), and printing the free name table, if free names were used (See Sections 5 and 16). If error messages appear on the control console (See TOP sudo, Section 7), then the type-in task \(O K\) is required before OUT is executed (See Section 25).

Upon leaving MTHAT, all user index registers are cleared to zero.
In order to safeguard against executing code in which assembly errors have occurred, the user should check all his labels using either the CHK or PRT sudos (See Section 9), and exit from assembly with the following code:
OUT \(\quad \mid 0 ;\) halt

OUT --..-; desired location

\section*{MTT sudo - mark transfer to}

\section*{1 parameter, nonlistable}

MTHAT executes a TRM at assembly time to the location named. If the user wishes to force the appearance of an assembly error, his subroutine should return to the mark. Otherwise his subroutine should return to the mark +1.

The user's subroutine should not use the same index registers as are used by MTHAT. Currently MIHAT uses index registers \(/ 30\) to /55, but this is subject to (gradual) change.

The MTT card image is printed on the assembly listing after execution of the MTT.

RET sudo - return
no paxameters
MTHAT returns control to the mark of the routine which called it. MTHAT must have been called by a routine by executing TRM \(\mid 37\).

\section*{9. CONTROLLING REGION AND LABEL DEFINITIONS}

See Section 5 for the distinction between regions and labels. The values of regions and labels may be defined either by the DEF sudo, or by the name of the region or label appearing in the label field of a card (See Section 3). Redefinition of the value of an already defined region or label can be done only by the DEF sudo, unless the region or label has been released by REL or LBL. All labels that are used in assembling code must be defined before they are released or before the end of assembly, but it is not an error for an unused label to remain undefined. DEF sudo - define 1 parameter, listable

The parameter is not just the usual expression, but instead is of the form:

\section*{variable \(=\) expression}
where the variable is either a region or label (or free name). The variable is defined to have the value of the expression, which must not itself contain undefined variables. The value of the definition, when truncated to an integer, must be between 0 and /177777 inclusive. If the variable is a label which was used prior to its definition, the value is filled in to the assembled words which used the label.

The location at which code is assembled may be altered by redefining \(A\).

CHK sudo - check labels
1 parameter, 1istable
The parameter is a single label. All the labels with the named identifier, from subscript 0 to the named subscript, are checked. An
```

error occurs if any of these labels has been used but not defined. If
the named subscript =0 or if there is no subscript, all the declared
labels of the named identifier are checked. Example:

```
    CHK L5, M;
Labels LO to \(L 5\) and all the \(M\) labels are checked.

LBL sudo - declare or release labels
1 parameter, listable
The parameter is a single label. If the named identifier is not a region, and if the identifier has not previously appeared in a LBL sudo, then the identifier is declared to name labels with subscripts from 0 to the named subscript. Example:

LBL \(\quad\) T7;
New Labels T0 to T7 are declared.

On subsequent use of the identifier in a LBL sudo, the labels with subscripts from 0 to the named subscript are checked as in the CHK sudo, then released to the undefined state for reuse. If the named subscript \(=0\) or if there is no subscript, all the declared labels of the named identifier are checked and released. An error occurs if the named subscript is higher than the original subscript used to declare the labels. Example:

\section*{LBL T7;}

Labels T0 to T7 are checked and released.
See the CON sudo, Section 15, for a discussion of the effect of the LBL sudo on the concordance.
```

REL sudo - release
1 parameter, listable

```
    The parameter is a single region or label. If the parameter is a
region, the named identifier is released for reuse either as a region
or for labels. If the parameter is a label, the single named label is
checked as in the CHK sudo, and then released to the undefined state
for reuse.

See the CON sudo, Section 15 , for a discussion of the effect of the REL sudo on the concordance.

PRT sudo - print labels
1 parameter, 1istable
The parameter is a single label. All the labels with the named identifier, from subscript 0 to the named subscript, are checked as in the CHK sudo. The values of all defined labels are printed. If the PUL switch is on, a special notation is made for those labels which are both undefined and unused. If the named subscript \(=0\) or if there is no subscript, all the declared labels of the named identifier are checked and printed. Example:
PRT L5, M;
Labels L0 to L5 and all the M labels are checked, and their values are
printed.

PUL sudo - print undefined and unused labels
no parameters
Each use of the PUL sudo reverses the state of the PUL switch. Initially the PUL switch is off. The PUL switch is used by the PRT sudo.

LEN sudo - label and enter
1 parameter, partially listable
The parameter is a single label. The named labels are checked and released as in the LBL sudo (listable), then a single word of all zeroes is assembled as in the ENT sudo (nonlistable). The printer is upspaced two blank lines before the LEN card image is printed on the assembly listing.
- - -

OUI sudo - 1abel, yes concordance
See Section 15.

NON sudo - label, no concordance
See Section 15.
10. ASSEMBLING G-21 INSTRUCTIONS

The following sudos assemble G-21 instructions for later execution. See also Section 6 and Section 26.
```

ENT sudo - enter

```
no parameters

A word of all zeroes is assembled. The printer is upspaced two blank lines before the ENT card image is printed on the assembly listing.

By convention, ENT is used at the beginning of a closed subroutine. The assembled word holds the return mark of the TRM calling the subroutine.

LEN sudo - label and enter
See Section 9.
```

SCP sudo - set character pointer
l parameter, nonlistable
Two LXP instructions are assembled which will set the monitor character pointer to the named column number at run time.

```
```

*** sudo - space for generated instruction

```
*** sudo - space for generated instruction
no parameters
```

A word of all zeroes is assembled. By convention, this word will be written over by an instruction that is generated at run time.
11. ASSEMBLING INTEGERS, ADDRESSES, AND BOOLEAN DATA LWD sudo - logic word

1 or 2 parameters, nonlistable; flag; mode

The first parameter is assembled and stored with an STL instruction. The first parameter may be an expression or a single undefined label. If the first parameter is an expression with value < $\$ 16$, or if it is an undefined label, then a second parameter may appear at the user's option. The second parameter must be an expression with value between 0 and $\$ 16-1$ inclusive. The second parameter automatically is multiplied by $\$ 16$ and united with the first parameter.

The flag and mode fields are scanned after the parameters have been evaluated. The flag, if specified, is united with whatever is in the flag field of the assembled word due to the parameter evaluation. The mode, if specified, overrides whatever is in the mode field due to the parameter evaluation.

WRD sudo - word
1 parameter, listable
The parameter may be an expression, a single undefined label, or a minus sign followed by a single undefined label. If the resulting value is $\geq 0$, it is assembled and stored with an STL instruction. If the resulting value is $<0$, it is assembled and stored with an $S T I$ instruction.

CLW sudo - complement logic word
1 parameter, nonlistable; flag; mode
The parameter must be an expression with all variables defined. The parameter is evaluated, then the flag and mode fields processed as in the LWD sudo. The bit-complement of the reault is assembled and ntored with an STL instruction. A FLG sudo (See Section 18) preceding this will be treated in the usual manner, not complemented.

ADC sudo - address constant
2 parameters, nonlistable; flag; mode
This sudo is processed as an OCA instruction with standard mode $=0$. By convention, this sudo is used to assemble addresses in the $15+1$ bit pattern of G-21 instruction word format.

CRS sudo - checksum
See Section 18.
12. ASSEMBLING FLOATING POINT NUMERIC DATA

The parameters to the sudos in Section 12 are not expressions, but instead are signed floating point numbers of the form: signed mantissa, followed by a signed integer power of 8 or 10. (8 for HPL and FPL, 10 for HPC and FPC.) The radix used in evaluating the mantissa and exponent is 8 for HPL and FPL, and 10 for HPC and FPC. The exponent begins with the character io for all four sudos. Examples: $+25.31_{15}-7$
.54
$-.66_{\text {ro }} 14$
$1_{n}+3$ (omitting the mantissa would result in a value $=0$ )
2.9 (HPC and FPC only....the octal number system does not include the digit 9)

HPL sudo - half precision octal
1 parameter, listable
The mantissa is evaluated as an octal number. If an exponent appears, it is evaluated as an octal integer and 8 is raised to that power. The resulting number is stored with an STS instruction.

FPL sudo - full precision octal
1 parameter, listable
The parameter is evaluated as in the HPL sudo and stored with an STD instruction.

HPC sudo - half precision decimal
1 parameter, listable
The mantissa is evaluated as a decimal number. If an exponent appears, it is evaluated as a decimal integer and 10 is raised to that power. The resulting number is stored with an STS instruction.

FPC sudo - full precision decimal
1 parameter, listable
The parameter is evaluated as in the HPC sudo and stored with an STD instruction.
13. ASSEMBLING ALPHANUMERIC DATA

## Alf sudo - alphanumeric

digit in card column 24; alphanumeric string starting in column 25
The digit determines how many words there are in the string, at 4 characters per word. A blank in column 24 means 1 word, a 0 in column 24 means 10 words. The words are assembled in the standard 8-bit, 4-character-per-word format.

NAM sudo - name
5-character string starting in card column 24; flag; mode
The standard 6-bit representation of the 5 characters is assembled into bits 0 to 29 of a word. Then the flag, if specified, is united with the word. The mode, if specified, overrides whatever is already in the mode field of the assembled word.

## 14. ALTERING THE LOCATION OR CONTENTS OF ASSEMBLY

Usually the location of asaembly is altered by redefining the value of the Current Location Counter, A. See the DEF sudo, Section 9.

RXA sudo - relocator

1 parameter, nonlistable
This sudo is used to assemble code which will eventually be transferred to some different locations for execution. The Current Location Counter, A, should be defined as the location at which the code will ultimately be executed. The RXA sudo sets the value of RXA, which initially is zero. Assembled code is stored at A+RXA.

The CPY, DMP, and SXX cudos automatically compensate for nonzero RXA. The CKS and PBC sudos do not compensate for nonzero RXA. It probably is an error to execute an OUT or MTT sudo to code that was assembled with nonzero RXA, and which has not been transferred to its ultimate location.

Al1 code assembled with nonzero RXA has the value of A+RXA and the value of RXA printed at the left edge of the assembly listing.

COA audo - continue on assembly
1 parameter, nonlistable
Two operations result from this sudo. First, RXA↔A+RXAparameter. Then $A$ parameter. The result is that $A$ is redefined to the value of the parameter, but RXA is adjusted so that storage at $A+R X A$ continues in sequence from the previous value of $A+R X A$.

## SXX sudo - set storage extracter

1 parameter, nonlistable
During assembly, the previously existing contents of $A+R X A$ are accessed with a CAL instruction and extracted with the storage extracter. The resulting bit pattern is united with the assembled word and the result is stored at A+RXA. The SXX sudo sets the storage extracter, which initially is zero.

FLG sudo - £1ag
See Section 18.
15. CONCORDANCE

The concordance is a cross-reference showing the card sequence numbers of every card that referred to a label, named a macro, or caused an assembly error. The concordance is generated during the assembly, and printed at the end of assembly as part of the OUT sudo (See Section 8). One word of memory is required to store each concordance reference. There is approximately one concordance reference per card input, on the average. The concordance is most useful if it is made on all labels, but it can be made on selected labels only, if storage apace ia scarce, by appropriate use of the OUI and NON sudos.

CON sudo - concordance
1 parameter, nonlistable
Concordance generation is initiated by the first appearance of the CON sudo. The parameter names the starting location for the table of references. Table entries continue in sequence unless the table is repositioned by another use of the $\operatorname{CON}$ sudo. If the parameter $=0$, concordance generation ceases. The OUT sudo prints whatever concordance has been generated.

An initial LBL sudo which declares new labels (See Section 9) is not included in the concordance. Labels declared by the LBL sudo are concorded, unless this state is changed by the OUI and NON sudos. Subsequent use of the LBL or REL sudos for releasing labels does not alter their current state of whether or not they are concorded.

```
REF sudo - reference
1 parameter, 1istable
```

This sudo creates a reference in the concordance table to every label in the parameter, whether or not the label currently is defined. Regions and constants are ignored, and the expression is not evaluated. The sudo is used for documentation purposes only.

OUI sudo - label, yes concordance
1 parameter, listable
The paramenter is a label, which is declared or released for reuse as in the LBL sudo (See Section 9): Subsequent references to the labels designated will be concorded, if a concordance is being generated at all.

NON sudo - label, no concordance
1 parameter, listable
The parameter is a label, which is declared or released for reuse as in the LBL sudo (See Section 9). Subsequent references to the labels designated will not be concorded.

## 16. FRBE NAMES

See Section 5 for a discussion of what free names are and how they are used.

LFN sudo - locate free name table
1 parameter, nonlistable
Free names may not be used until a table for their storage has been located. The parameter is the base address of the table. Free names of 2, 3, or 4 characters length require 1 word of storage. Free names of $5,6,7$, or 8 characters length require 2 words of storage. The LFN sudo may be used only once in a program.

PFN sudo - print the free name table no parameters

The free name table is printed in both numeric and alphabetic order. It is not an error if no free name table exists. The free name table also is printed automatically by the OUT sudo (See Section 8).
17. MACROS

Each macro consists of several card images that are stored in the computer memory during the macro declaration. All the card images of the macro may subsequently be read back and processed by MTHAT, at each appearance of macro call card. The macro call card has the name of the macro in the opcode field (See Section 3), and may have several actual parameters to the macro in the parameters, flag, and mode fields. The actual parameters in the parameters field of the macro call card correspond to the formal parameters $A>, B>, Q, D>, E$, and $F>$ that may be used in the coding of the macro declaration. The "greater" variables may also be used in other parts of an MrHAT program, but their primery use is as formal parameters to macros.

The greater variables are loaded by the up-to-6 actual parameters appearing on macro call card or VAR sudo card. The actual parameters are separated by comase, and are loaded into $A>, B>, C, D>, E$, and $F>$ in that order. Any actual parameters omitted at the end of the card, or left blank between commas, leave the corresponding greater variables unchanged. If an actual parameter consists of an expression other than a single region or label, then the expression is evaluated immediately and its value is loaded into the proper greater variable. In subsequent use, the greater variable is treated as a constant. If the actual parameter consists of a single region or label, then the name of the region or label is loaded into the proper greater variable. In subsequent use, the actual parameter is treated as though it were the name of that region or label, and is given whatever meaning is currently assigned to that name.

It also is possible to parameterize the flag and mode fields for use in macros or elsewhere. There exist within MTHAT two variables
called the "flag temp" and the "mode temp". These variables are loaded whenever a macro call card of VAR sudo card is processed, and are read whenever any other card is processed.

Each of these variables may be in any one of five states:
0
1
2
3
blank
The rules for loading the flag and mode temps are summarized in the following table.

FLAG PUNCH/ MODE PUNCH / PREVIOUS STATE OF TEMP / NEW STATE OF TEMP

| 0, 1, 2, 3 | 0, 1, 2, 3 | immaterial | 0, 1, 2, 3 |
| :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { A, B, C, D, } \\ E, F \end{gathered}$ | $\begin{gathered} \text { A, B, C, } \mathrm{D} \\ \mathrm{E}, \mathrm{~F} \end{gathered}$ | immaterial | $\begin{aligned} & A>\wedge 3, B>\wedge 3, \\ & C \wedge \wedge, B>\wedge 3, \\ & E>\wedge 3, F>\wedge 3 \end{aligned}$ |
| * | * | 0, 1, 2, 3, BLANK | 0, 1, 2, 3, BLANK |
| fllegal | + | 0, 2 | 2 |
|  |  | 1, 3 | 3 |
|  |  | BLANK | BLANK |
| 11legal | - | 0, 2 | 0 |
|  |  | 1, 3 | 1 |
|  |  | blank | blank |
| blank | blank | immaterial | BLANK |

The rules for reading the flag and mode temps are sumarized in the following table.

| FLAG PUNCH | MODE PUNCH | STATE OF TEMP | EFFECTIVE FLAG OR MODE |
| :---: | :---: | :---: | :---: |
| 0, 1, 2, 3 | 0, 1, 2, 3 | immaterial | 0, 1, 2, 3 |
| $\begin{gathered} \text { A, B, C, D, } \\ \text { E, F } \end{gathered}$ | $\begin{gathered} A, B, C, D, \\ E, F \end{gathered}$ | immaterial | $\begin{aligned} & A>\wedge 3, B>\wedge 3, \\ & \subset \wedge \wedge, D>\wedge 3, \\ & E>\wedge 3, F>\wedge 3 \end{aligned}$ |
| * | * | 0, 1, 2, 3 | 0, 1, 2, 3 |
|  |  | BLANK | 0 flag , standard mode |
| 11lega 1 | + | 0, 2 | 2 |
|  |  | 1, 3 | 3 |
|  |  | BLANK | standard mode V2 |
| 111egal | - | 0, 2 | 0 |
|  |  | 1,3 | 1 |
|  |  | BLANK | $s$ tandard mode $\wedge 1$ |
| blank | blank | immaterial | 0 flag, standard mode |

where "standard mode" refers to the standard mode of the card being processed.

VAR sudo - greater variable
6 parameters, nonlistable; flag; mode
The greater variables and flag and mode temps are loaded as described above.


#### Abstract

MAD sudo - macro administration

3 parameters, nonlistable This sudo may be used at most once in a program, which must be before the first MAC sudo. The first parameter specifies the maximum number of macros to be declared, and must be $\leq 300$. The size of the MTHAT label table is incremented by twice this value. The second parameter is the location where the card images that comprise the macros are to be stored. Each card image requires 21 words of storage. The third parameter, if it appears, is the maximum number of blocks that can be pushed at any given time by the $P S H$ sudo. These blocks each require 20 words of storage, and are stored at the locatiun designated by the second parameter. Storage of macro card images starts after the end of these blocks.


MAC sudo - declare a macro macro name in card columns 26 to 28

This sudo starts a macro declaration. Images of the following cards are stored in core, to be processed when the macro is called. Macro calls may be stored within the declaration of another macro, in which case the macro call card and all the card images of the macro being called are stored again as part of the macro being declared. This allows nesting of macros to indefinite depth. Macros may not call themselves.

Any cards may appear in a macro declaration except the following: LFN, MAC, RET, TB1, TB2, ZRO. Each macro may consist of a maximum of 255 card images.

FIN sudo - finish macro declaration
character in card column 24
This sudo terminates the declaration of a macro. Until this card is processed, the macro may not be called. If the character in column 24 is the digit 0 , then all the greater variables are cleared to zero. Otherwise the greater variables remain unchanged. The FIN card image is printed twice on the assembly listing, because the card is both stored as part of the macro declaration, and processed to termInate the declaration. However, the label field of the FIN card is processed only during a macro call. The LIS sudo, also terminates macro declarations, but it is not recomended for this purpose. - - -

The remaining sudos in this section are designed to simplify the task of using MTHAT as a macro assembler. The BRA, BRV, and BRD sudos may appear only inside macros. These three sudos cause branching of the card processing by MTHAT. That is, after processing one of these sudos, the next card processed by MTHAT may not be the card that appears immediately after the sudo. The next card processed is called the "destination card." Destination cards are marked by having a "destination number" punched in column 3. The destination number may be a digit, $0,1,2,3,4,5,6,7,8,9$, or it may be the character $n$. Only cards within macros, including the FIN card, may be destination cards. If several macros are nested together, the card branching may go in and out of the inner macros, but may not leave the outermost macro. In other words, the destinations must be nested within the outermost macro. The destination numbers are treated as local to the outermost macro, and may be reused in any other disjoint macro. Special precautions must be observed when a destination lies within the scope of an ITR sudo. (See Section 19)

BRA sudo - unconditional branch

1 parameter, nonlistable
This sudo may appeax only inside macros.
The value of the parameter is the destination number of the next card to be processed by MTHAT. If the parameter is blank, the next card processed will be the card appearing immediately after the BRA card.

BRV sudo - conditional branch on value
4 parameters, nonlistable
This sudo may appear only inside macros.
The first parameter is evaluated and truncated to a 32-bit signed integer. The resulting value determines which of the three possible destinations, in the three following parameters, will be branched to by MTHAT. If the value is positive, MTHAT will branch to the first destination. If the value is zero, MTHAT will branch to the second destination. If the value $1 s$ negative, MTHAT will branch to the third destination.

Only the actual destination parameter is evaluated by MTHAT. If the parameter is blank or absent, the next card processed will be the card appearing immediately after the BRV card.

If the value of the destination parameter is not between 0 and 10 , inclusive, then an assembly error will result. This may be used to force the appearance of an error message as the result of an assemblytime test.

BRD sudo - conditional branch on definition
3 parameters, nonlistable
This sudo may appear only inside macros.

The firgt parameter must be one of the terms listed in Section 4 . However, the BRD sudo is of use only if the first parameter is a term of Type $7,8,9$, or 10 .

If the term currently has a defined value, then MTHAT will branch to the destination indicated by the second parameter. If the term currently is undefined, then MTHAT will branch to the destination indicated by the third parameter.

Only the actual destination parameter is evaluated by MTHAT. If the parameter 18 blank or absent, the next card processed will be the card appearing immediately after the BRD sudo.

If the value of the destination parameter is not between 0 and 10 , inclusive, then an assembly error will result. This may be used to force the appearance of an error message as the result of an assemblytime test.

PSH sudo - push down macro parameters
no parameters
The greater variables, flag temp, and mode temp are pushed down, in a block. The maximum number of blocks that can be pushed at any given time is determined by the third parameter to the MAD sudo.

POP sudo - pop up macro parameters
character in column 24 of card

The last block pushed by the PSH sudo is popped up. The flag and mode temps are restored, and some of the greater variables are restored. A letter in column 24 of the card indicates the first of the greater variables to be restored. For example, if column 24 contains the letter $C$, then $C, D>B>$, and $F>$ are restored, and $A>$ and $B>$ are left alone. If column 24 is blank, then all the greater variables are
restored. If column 24 contains the digit 0 , then none of the greater variables are restored (but the flag and mode temps are restored).

SSC sudo - subscript
1 parameter, nonlistable
The parameter must be one of the terms listed in Section 4, except not a term of Type 6. However, the SSC sudo is of use only if the parameter is a term of Type 9 or 10.

If the parameter is a constant, then the subscript variable $V$ (see Section 19) is set to the value of the parameter. If the parameter is a variable, then $V$ is set to the subscript of the variable, whether or not the variable currently has a defined value. This sudo may be used to find the subscript of a label corresponding to a free name.
18. ERROR DETECTION AND CORRECTION

```
Assembly errors detected by MHAT immediately terminate processing of the card on which they ware found. The error measage may be printed on the assembly listing, or typed on the control console for correction by the operator, or both, depending on the second parameter to the TOP sudo (See Section 7). If error output appears on the control console, then the card column number at which the error was detected, and the current value of \(A\), also are typed out. A single card image is requested from the operator, to correct the error. If more than one card is required to correct the error, then the first card image typed in may be the TYP audo (See Section 25). If a concordance is being generated, a reference is created for each detected assembly error.
In order to prevent a waste of computer time in the assembly of "garbage", MHAT assembly automatically halts if an average error rate of one error for every four cards is maintained.
```

DBG sudo - debug
no parameters
If this sudo appears anywhere in an MTHAT assembly, the monitor trace subroutine $\mid 72$ is enabled. This subroutine will trace all 2-flagged instructions in the assembled code.

FLG sudo - flag
1 parameter, nonlistable
The parameter must evaluate to $0,1,2$, or 3 . This value will be united with the flag field of the next word assembled. A blank parameter is given the value 2. An error occurs if FLG 1 or FLG 3 precedes
a G-21 instruction word, or if any nonzero flag precedes the CKS or LC8 sudos.

Because operand assembly (OA) instructions are not traced, placing a FLG sudo before an OA instruction causes the next non-OA instruction to be traced.

ERR sudo - errors no parameters

A count of all the errors which have not been corrected at the control console is printed. ERR card images always are printed, independent of the parameters to the TOP sudo (See Section 7).

ZEC sudo - zero the error counter no parameters

This card is processed in the same manner as ERR sudo cards, and then the counter of uncorrected errors is set to zero.

PIE sudo - process if errors
no parameters
This card is processed in the same manner as ERR sudo cards. If the counter of uncorrected errors is nonzero, the next card following is processed in the normal manner. If the counter of uncorrected errors is zero, processing of the next card is bypassed. The card image is printed on the assembly listing with arrows to indicate bypassing. Normal MTHAT processing resumes with the second card after the PIE sudo.

The PIE sudo is used to prevent execution of code that contained assembly errors. For further discussion, see the OUT sudo, Section 8.

CKS sudo - checksum
2 parameters, partially listable
The two parameters are the starting and ending locations for a checksum (listable) formed using ADL. A single word is assembled (nonlistable) which contains the checksum.

CSR sudo - check status report
1 parameter, nonlistable
Changes made to the MTHAT system are summarized in a one-line status report. The CSR sudo causes printing of the status report on the assembly listing. MTHAT also has a "change rumber", which is incremented whenever aignificant change is made to the system. If a parameter appears with the CSR sudo, the parameter is tested against the change number. An error occurs if the parameter is less than the change number, which indicates that some of the user's code may be incorrect because of a change in the system. If the parameter is blank, no test is made.
19. ASSEMBLY-TIME ITERATION

The character $V$, called the subscript variable, serves a special function in the evaluation of constants and variables. Its primary use is for assembly-time iteration, but it may be used elsewhere if so desired. $V$ is a double precision variable that may be intermixed with digits in a constant or in the subscript of a variable. Evaluation is performed from left to right, with the evaluated portion to the left of $\checkmark$ being multiplied by the value of $V$, and then the portion to the right of $V$ being evaluated and added to form the final result. In the following examples, assume that the current value of $V$ is 5.

| PARAMETER | value |
| :---: | :---: |
| V | 5 |
| $\cdot v+1$ | 6 |
| LV | L5 |
| LV +1 | L5 + 1 |
| \$ | \$5 |
| V1 | 6 |
| /V22 | $/ 27=5+/ 22$ |
| LV1 | L6 |
| 2 V | 10 |
| W | 25 |
| 2 V 1 | 11 |
| 2VIV | 55 |
| 2vivl | 56 |
| L2V1V1 | L56 |
| $/ 10 \vee 17$ | $/ 67=/ 50+/ 17$ |

SET sudo - set $V$
1 parameter, nonlistable
The double precision subscript variable $V$ is set to the value of the parameter.

ITR sudo - iterate
5 parameters, nonlistable
This sudo allows for iterative processing of card images during assembly time. Call the parameters $\mathrm{N}_{1}, \mathrm{~N}_{2}, \mathrm{~N}_{3}, \mathrm{~N}_{4}, \mathrm{~N}_{5}, \mathrm{~N}_{1}$ is the value which $V$ is assigned before iteration begins. $N_{1}$ is evaluated and stored into $V$ before the other parameters are evaluated. $N_{2}$ is the value of the increment to $V$ which automatically occurs at the end of each iteration cycle. $N_{1}$ and $N_{2}$ may be any value, positive or negative, and are stored in double precision. $N_{3}$ is the number of cycles of iteration to be performed. $N_{3}$ must be a non-negative integer. $\mathrm{N}_{4}$ is the number of cards composing a cycle of the iteration. $\mathrm{N}_{4}$ must be a strictly positive integer. $N_{5}$ is the base address of a region in memory where $\mathrm{N}_{4}$ card images may be stored until the interation is completed. Each card image requires 21 words of storage space.

The following cards may not appear within the scope of an iteration (that is, among the $\mathrm{N}_{4}$ cards following the ITR card): ITR, LIS, MAC, TB1, or macro call cards.

The parameters on the ITR card are evaluated only once, before iteration begins.

If the ITR sudo appears inside a macro, then the 5 th parameter, $N_{5}$, must be omitted, since the card images will be stored in the computer memory as part of the macro declaration. The scope of the iteration must be properly nested within the outermost macro which contains the ITR card as part of its declaration. However, the scope of the iteration may extend past the ead of a macro nested within the outermost macro. For example, a piece of (useless but) valid code might be:

| MAC | ABC |  |
| :--- | :---: | :--- |
| COM | COMMENT 1 OF ABC |  |
| ITR | $0,0,6,3 ;$ USELEßS ITERATION |  |
| COM | COMMENT 2 OF ABC |  |
| FIN |  |  |
| MAC | XYZ |  |
| COM | COMMENT 1 OF XYZ |  |
| ABC |  |  |
| COM | COMMENT 2 OF XYZ |  |
| COM | COMMENT 3 OF XYZ |  |
| FIN |  |  |

because the declaration of macro XYZ is expanded by MTHAT to:

| MAC | XYZ |
| :--- | :--- |
| COM | COMMENT 1 OF XYZ |
| ABC |  |
| COM | COMMENT 1 OF ABC |
| ITR | $0,0,6,3$; USELESS ITERATION |
| COM | COMMENT 2 OF ABC |
| FIN |  |
| COM | COMMENT 2 OF XYZ |
| COM | COMMENT 3 OF XYZ |
| FIN |  |

Caution must be exercised when using the branch sudos BRA, BRV, and BRD (see Section 17) in conjunction with ITR inside a macro. Do not branch into the scope of the iteration from outside the scope unless you previously branched out from inside while the iteration still was in progress. Otherwise erratic card processing might occur.
20. PARALLEL TABLES

Parallel tables are two or more tables for which the entries correspond, such as a table of task names and a table of corresponding subroutine locations for executing the tasks. It is possible to put the corresponding entries for two tables on a single card, both to help make the tables self-commenting and to prevent accidental displacement of the entries in one of the tables. If more than two parallel tables are desired, entries for the first two tables are put on one card and corresponding entries for the remaining tables are put on another card that follows immediately.

The two sudos TB1 and TB2 are intended to precede and follow the cards which contain the table entries, in order to delimit the scope of parallel table processing. The sudo TB3 is used on data cards appearing between TB1 and TB2, only if there are three or more parallel tables.

TB1 sudo - table 1

1 parameter, nonlistable

All cards following the TB1 card, except TB3 cards, will be processed in the normal manner, like any other MTHAT cards. Also, the card images will be stored in the computer memory, starting at the location named in the parameter. Each card image requires 21 words of storage space. The following cards may not appear between TB1 and TB2 sudos: ITR, LIS, MAC, OUT, RET, TB1, and macro call cards.

The label field of TB3 cards will be processed as usual, but otherwise TB3 cards will be treated as comment cards.

```
TB2 Sudo - table 2
2 parameters, listable
    AND
TB3 sudo - table 3
variable format
The card images that have been stored in core are read back and processed again, with print off, in order to form the second parallel table:
1. TB3 cards are ignored entirely.
2. Only a special field is examined on the cards that are processed. This field starts with a control column (col. 68) and extends to the last column (col. 80). The remainder of the card is ignored.
3. If the control column contains \(a+\) or -, then a single expression is expected in the field. The + or - in the control column is considered part of the expression. The expression is assembled as is done by the WRD sudo. The expression may have all variables defined, or it may consist of \(a+\) or - in the control column and a single undefined 1 abel.
4. If the control column contains a digit, then that number of alphanumeric words are assembled. The characters for the words are taken from the field, starting in the first column after the control column, and packed 4 characters per word. The number of words specified by the digit in the control column must not require more than 3 characters past the last column in the field. That is, \(1 \leq\) digit \(\leq\)
\(\downarrow\) [[number of last column +3 - number of control column]/4].
```

Characters taken from beyond the last column of the field are assembled as blanks.
5. If the control column contains the letter $A$, then a single expression is expected in the remainder of the field, starting In the first column after the control column. The Current Location Counter, $A$, is redefined to have the value of this expression.
6. If the control column contains any character except the characters listed in (3), (4), and (5) above, then the card image is ignored.

Processing continues on these cards until the TB2 sudo card is read again. Columns 68 to 80 of the TB2 card are not processed. At this point, columns 24 to 67 of the TB2 card are scanned for a pair of parameters. If the parameters are not found, parallel table processing terminates.

If the parameters are found, then the first parameter is interpreted to be the number of a control column, and the second parameter is interpreted to be the number of the last column of the field. The card images that have been stored in memory are read back and processed again, with print off, in order to form a third parallel table. This time only the TB3 cards are processed; all other cards are ignored. Processing follows conventions (2) to (6) above, where the number of the control column and the number of the last column are determined by the expressions on the TB2 card.

If the $T B 2$ card contains more pairs of expressions, then 4 th, 5 th, etc. parallel tables are formed from the data on the TB3 cards.

## 21. CONTROLLING INPUT CARDS

Card images may be obtained from the control console (See Section 25), the card reader, disc, tape, or the computer memory (for macros, assembly-time iteration, or parallel tables). Each card image read by MPHAT is sequence numbered. The MTHAT sequence number is printed on the assembly listing to the left of the card image, and to the left of the current value of $A$. Sequence numbers appearing to the right of the card image were assigned by the AND system.

CSS sudo - card source switch

3 parameters, nonlistable
Call the parameters $N_{1}, N_{2}, N_{3}, N_{1}$ and $N_{2}$ are monitor logical file table entry numbers or else blank; $N_{3}$ may be any expression or blank. The CSS sudo operates as follows:
(1) Record the source for subsequent card images in logical file table entry $N_{1}$ (if the parameter is blank, no write occurs).
(2) Read from logical file table entry $N_{2}$ the source for subsequent card imagea (if blank, no read).
(3) Reset the source for subsequent card images as follows:
$N_{3}$ blank, no reset. Subsequent card images come from the source read in (2) above, or from the previous source if $\mathrm{N}_{2}$ is blank.
$\mathrm{N}_{3}<0$, subsequent card images come from the beginning of AND scratch. The information obtained from the read operation in (2) above is lost.
$N_{3}=0$, subsequent card images come from the card reader. $\mathrm{N}_{3}>0$, subsequent card images come from disc or tape, starting from the source point read in (2) above, or from the previous disc or tape source if $N_{2}$ is blank.

In order to understand the operation of CSS, it is necessary to know that the monitor has a single switch which determines whether carda are read from the card reader or from either disc or tape. The monitor also has a single pointer to the location of the next card image coming from disc or tape. This pointer is not altered when cards are read from the card reader. Both the switch and the pointer may be saved by storing their values in any one of the logical file table entries.

BYP sudo - bypass
3 parameters, nonlistable
Call the parameters $N_{1}, N_{2}, N_{3}$. Normal MTHAT processing of the card following the BYP card is bypassed if the logical proposition $\left[N_{1}>N_{2}\right] \equiv\left[N_{3} \neq 0\right]$ is true. If the proposition is false, the follow. ing card is processed as usual. Arrows printed on the assembly listing indicate that the card has been bypassed. The parameters are evaluated as signed integers.

BNC sudo - bypass N cards
1 parameter, nonlistable
The parameter specifies the number of cards following the BNC card whose processing is to be bypassed. Arrows printed on the assembly listing indicate that the cards have been bypassed.

PIE sudo - process if errors
See Section 18.

CRD audo - card input
See Section 25.

TYP sudo - control console input
See Section 25.

BRA sudo - unconditional branch
See Section 17.

BRV audo - conditional branch on value
See Section 17.

BRD sudo - conditional branch on definition
See Section 17.
22. Saving assembled code

Assembled code may be saved on row-binary cards by the PBC sudo, or on AND records by MTHAT subroutine ' 22 (See Section 24). There is no sudo for executing ' 22 , but the proper calling sequence may be set up and executed by an MTT (See Section 8) if desired.

PBC sudo - punch binary cards
3 parameters, nonlistable
The first two parameters are the starting and ending locations of a region of the computer memory whose contents are punched on row-binary cards. If a third parameter $=1$ appears, the MTHAT symbol table also is punched. Punching the symbol table allows later alteration of the program using the original regions and labels, when the program is read back by RBC.

The use of a concordance, free names, or macros affects the use of the symbol table. If the symbol table is punched by PBC when any of these features are in use, the user must also include additional PBC sudos which punch the concordance table, free name table, and macro card images.

RBC sudo - read binary cards
no parameters
The cards punched by the PBC sudo are read back into the locations from which they were punched. If the MTHAT symbol table was punched by PBC, it is read back and completely replaces the current MTHAT symbol table. One RBC sudo is required for each use of the PBC sudo.

[^1]23. USER-DECLARED SUDOS

Uaually any code the user wishes executed at assembly time can be written so that it is entered by the MIT sudo (See Section 8). However, MTHAT has a sudo trap feature which allows the user to write his own sudos. Sudo processing is so intimately connected with the internal mechanism of MTHAT, that the user is strongly urged to contact the person maintining the MTHAT system before attempting to write his own sudios.
24. RUN-TIME FEATURES

Some of the subroutines and tables used by MTHAT during assembly may also be of use to the user during run-time. Switch '21 and subroutines ' $18,{ }^{\prime} 19,{ }^{\prime} 22,{ }^{\prime} 23$, and ' 24 are independent of the presence of the remainder of the MTHAT system. They are located at the bottom of user memory, and extend up to location ${ }^{\mathbf{\prime}} \mathbf{2 0 - 1}$. The remaining tables and subroutines are scattered throughout the MTHAT system. See Section 33 for complete list of available tables and subroutines.

Subroutine '17: Convert (ACC) to label for symbolic disassembly. Input in ACC: A number, presumably an address. Output in ACC: The label corresponding to that address. Operation: If $1 \leq$ input $\leq \$ 16$, then a search is made through the label table for the first label whose value $=\downarrow$ [input]. If found, the subroutine exits to the mark +1 with the label in the ACC as follows:

Bits 0 to 7: alphanumeric representation of the identifier Bits 8 to 21: subscript stored as an integer The search is performed in the same order as labels are printed in the concordance. If no such label is found, or if the input is not within the specified range, the subroutine exits to the mark with garbage in the ACC.

Storage: Some parts of MTHAT, the label table, and index registers /30 and /31.

```
Subroutine '18: Write a logical file table entry.
Input in index register /30: A logical file table entry number.
```

Operation: The contents of the switch and pointer in the monitor which determine the source of aubsequent card images are written into the logical file table entry (See CSS sudo, Section 21).

Exits: RED exit to mark, error, no write performed GREEN exit to mark + 1

Storage: Below location ' 20 , and index register / 30

Subroutine '19: Read a logical file table entry.
Input in index register /30: A logical file table entry number. Operation: The contents of the logical file table entry are read into the monitor switch and pointer which determine the source of subsequent card images (See CSS sudo, Section 21).

Exits: RED exit to mark, error, no read performed GREEN exit to mark +1

Switch '21: Upper core request.
This switch is set by the 64 K sudo (See Section 27) and interrogated by subroutine ' 24 . Its value is 0 if upper core memory has not been requested or if the request was denied. Its value is 1 if the request was granted.

Subroutine '22: Write a disc or tape file.
Several disjoint regions of memory are written to disc or tape. They may be read back by ' 23 . The file must have been set up and named in one of the monitor logical file table entries. A buffer region of length $=1$ block [ 320 words] must be provided. This subroutine uses index registers $/ 30, / 31$, and $/ 32$ for temporary storage. Calling sequence code:

```
    Word 0: TRM '22
    Word 1: logical file table entry number
    Word 2: location of buffer region
    Following pairs of words [at least 1 pair]:
        lat word: utarting location of data region
    to be written
    2nd word: ending location +1 of data region
        to be written
    Next word: RED exit error instruction
    Next word: GREEN exit instruction and subsequent code
The word pairs designating regions to write are assumed to continue
until a word is found with some nonzero bits in bit positions }16\mathrm{ to
31. This word is assumed to be the RED exit error instruction.
Therefore, the RED exit error instruction may not be an OCA mode 0.
If the subroutine returns through the RED exit, the accumulator con-
tains an integer indicating the error, as follows:
    0 error in calling sequence
    1 error in logical file table entry
    2 attempt to write into protected area
    3 insufficient space in file
The pairs of words in the calling sequence which designate regions are
altered by the subroutine.
Subroutine '23: Read a disc or tape file.
A file written by ' 22 is read back into the memory locations from which it was written. The file must have been set up and named in one of the monitor logical file table entries. A buffer region of
```

```
length =1 block [ }320\mathrm{ words] must be provided. This subroutine uses
Index registers / 30, /31, and /32 for temporary storage. Calling
sequence code:
    Word 0: TRM '23
    Word 1: logical file table entry number
    Word 2: location of buffer region
    Word 3; RED exit error instruction
    Word 4: GREEN exit instruction and subsequent code
If the subroutine returns through the RED exit, the accumulator con-
tains an integer indicating the error, as follows:
    0 error in calling sequence
    1 error in logical file table entry
    2 data in file was not written by '22
    3 read operation completed, but checksum failed
Subroutine '24: Test if (ACC) is within user memory.
Input in ACC: A number, presumably an address.
Exits: Mark, (ACC) is not within user memory.
    Mark +1, (ACC) is within user memory.
Output: Input (ACC) is undisturbed.
```

25. CONTROL CONSOLE INTERACTION

System programmers who use the control console for on-line debugging can take advantage of the control console features of MTHAT. The TOP sudo (See Section 7) allows error messages to be typed automatically on the control console, and the errors to be corrected by typed-in card images. The OPA sudo allows predetermined messages to be typed out, and the PFC sudo allows octal parameters to be typed in. Card source switching may be accomplished by the CRD and TYP sudos when MTHAT $1 s$ processing cards, or by the, CRD and, TYP type-in tasks in the extended monitor type-in task table. Preprogrammed halts for execution of type-in tasks may be accomplished by the MON sudo. Unscheduled halts for execution of type-in tasks may be accomplished by the , MON type-in task.

Card images typed in from the control console may consist of up to 40 characters, including blanks and commas. The first 3 comas scanned act as field delimiters, like the TAB keys on a typewriter The characters typed in before the first comma are shifted to card columns starting at column 4 , the beginning of the label field on the card. The first comma typed in does not appear as part of the card image, but ingtead acts as a tab to colum 15 , the beginning of the opcode field. The second comma acts as a tab to column 20 , the mode field. The third comma acts as a tab to column 24, the beginning of the parameters field. All subsequent commas typed in are processed the same as any other character, and appear in the card image. For example, to type in the card image:

L3 CLA $0 \quad 5, \mathrm{X} 7$;
the characters to type in are:
L3, CLA , 0, 5, X7;

```
    When card images are being typed in from the control console for
listing only (See the LIS sudo, Section 7), commas are not given the
special function described above. All commas appear as part of the
card image.
    See Section 18 for a discussion of error messages on the control
console.
    During an MTHAT assembly, the standard monitor type-in task table
is extended to include the tasks described below. The task names must
not be typed in after the end of assembly unless the MTHAT system re-
mains undisturbed in the computer memory. The tasks are:
,CRD Enter MTHAT, read cards from the card reader, disc, or
                    tape.
,TYP Enter MTHAT, get card images from the control console.
,PAG Page the line printer, enter MTHAT, get card images from
                    the control console.
,MON RET Leave a note for MTHAT to enable monitor type-in when
                                    MTHAT has completed processing the current card.
OR Process the current card (See the OUT sudo, Section 8).
CRD sudo - card input
no parameters
Subsequent card images are taken from the card reader, disc, or tape.
TYP sudo - control console input
no parameters
Subsequent card images are taken from the control console.
```

```
MON sudo - monitor
no parameters
Normal card processing is halted. When the control console is free from any input or output tasks initiated previously, the monitor type-in is enabled.
OPA sudo - operator alert
alphanumeric string in card columns 25 to 80
The string is typed out on the control console on a full interrupt basis, while other card processing by MTHAT continues.
PFC sudo ~ parameters from console
2 parameters, nonlistable
The first parameter, whose value must be either 1 or 2 , \(1 s\) the number of octal parameters to be typed in from the control console and stored in \(\mid 62\) and \(\mid 62+1\). The second parameter is the location of a closed subroutine to be executed automatically when type-in has been completed. If the second parameter is absent, blank, or zero, no subroutine will be executed when type-in has been completed.
The type-in is done on a full interrupt basis; while other card processing by MTHAT continues. It is the responsibility of the user to check that type-in has been completed before attempting to utilize the typed-in parameters. This may be done by an MTT to a subroutine which in turn calls on \(\mid 56\), the control console busy test in the monitor. An MTT directly to \(\mid 56\) would cause an assembly error, because \(\mid 56\) would return to the RED exit of the MTT sudo (See Section 8).
```


## TOP sudo - type or print

See Section 7.

PVE sudo - print value of expression
See Section 7.

OUT sudo - leave MTHAT
See Section 8.
26. HARDWARE REGISTERS AND LINE COMMANDS

MTHAT has a single table ' 11 of register and line command mnemonics. It is the responsibility of the user to guard against conflict between these mnemonics and the free names in his code, when writing code that utilizes any of the sudos in this Section.

ERA, ERO, EXR, and LDR audos
2 parameters, nonlistable; flag; mode
These sudos assemble the G-21 instructions ERA, ERO, EXR, and LDR. The standard mode is mode 2 . The first parameter, which is assembled into the address field of the G-21 instruction word, is processed in a manner identical to other G-21 instructions (See Section 6). The second parameter, which is assembled into the index field of the G-21 instruction word, is compared with the mnemonics in MTHAT table '11. If it is a memonic, the corresponding value is loaded into the index field. If it is not a memonic, the second parameter is then processed in a manner identical to other G-21 instructions.

TC8, TD8, and RD8 sudos
2 parameters, nonlistable; flag; mode
These sudos assemble the G-21 instructions TC8, TD8, and RD8. The instructions are used as the second word of block input/output commands. The standard mode is mode 0 . All other comments pertaining to the ERA, ERO, EXR, and LDR sudos also apply to the TC8, TD8, and RD8 sudos.

TLC sudo
2 parameters, nonlistable; flag; mode
This sudo assembles the G-21 instruction TLC. The first parameter, which is assembled into the address field of the G-21 instruction word, is compared with the mnemonics in MTHAT table '11. If it is a mnemonic, the corresponding value is loaded into the address field, and the standard mode of the instruction is mode 0 . If it is not a mnemonic, the first parameter is then processed in a manner identical to other G-21 instructions, and the standard mode of the instruction is mode 2 . The second parameter, which is assembled into the index field of the G-21 instruction word, is processed in a manner identical to other G-21 instructions (See Section 6).

LC8 sudo - 8-bit line commands

1 parameter, 1istable

This sudo assembles line commands and numeric data in 8-bit characters for transmission over the communication line. If the parameter is a mnemonic from MTHAT table 'll, the corresponding value is packed in a single 8-bit character. If the parameter is an expression, the value of the expression is packed in two characters and numeric flags added. An error occurs if the value of the expression is not between 0 and / 7777 inclusive.

The resulting characters are assembled four per G-21 word. If the number of characters generated is not an integer multiple of 4 , the remaining characters are packed left-justified and the rest of the last word made zero.
27. OTHER SUDOS

ZRO sudo - zero memory
All of user memory past the current end of the MTHAT label table is set to zero. If an upper core request has been granted, upper core user memory also is set to zero. In particular, this sudo will destroy the data stored in a concordance table, free name table, or stored macro card images.

-     -         - 

CPY sudo - copy
2 parameters, listable
Call the parameters $N_{1}, N_{2}$. The $N_{2}$ words last assembled are repetitively copied into the next $N_{1}$ locations. If $N_{2}=0$, then zeroes are stored into the next $N_{1}$ locations. $N_{2}$ must be nonnegative. Both parameters must appear on the CPY card. If the last $N_{2}$ words contain any undefined labels, these will not later be defined in the copies.

Example:

$$
\begin{array}{lll}
\text { L1 } & \text { WRD } & 5,7 ; \\
& \text { CPY } & 9,2 ;
\end{array}
$$

is the same as;

$$
\begin{array}{ll}
\text { L1. WRD } & \text { 5,7; } \\
& \text { WRD } 5,7,5,7,5,7,5,7,5 ;
\end{array}
$$

SIZ sudo - size of MTHAT no parameters

The subscript variable $\vee$ (See Section 19) is set to the current size of MTHAT, including the MTHAT label table. After executing the SIZ sudo, ' $16+V=$ the address of the first location after the current end of MTHAT and the label table.

64 K sudo . request use of upper core memory
no parameters
Before the 64 K sudo is executed, switch ' 21 contains the value 0 . If the request is granted, the contents of ' 21 are set to 1 . If the request is denfed, the contents of ' 21 remain at 0 and an assembly error results.

OPT sudo - option
3 parameters, nonlistable
This sudo just saves an MTT to the monitor option subroutine, 134. The three parameters are the same as in the option writeup.


```
073 STZ 
165 SUA 2
065 SUB 2
0 7 5 ~ S U L ~ 2 ~
125 SUN 2
022 SUX 2
026 SXT . 2
140 TC8 0 (See Section 26)
117 TDC 2
100 TD8 0 (See Section 26)
157 TLC 0 or 2 (See Section 26)
017 TRA 0
037 TRE 0
177 TRM 0
175 UCL 2
155 UNL 2
010 XEQ 2
036 XMT 2
016 XPT 2
```

29. LIST OF ALPHANUMERIC CHARACTERS

| G-21 <br> Internal <br> Representation | G-21 Character | Punch Card Hole Pattern | Mode1 29 <br> Keypunch Character |
| :---: | :---: | :---: | :---: |
| 00 | Space | No Punch | Space |
| 01 | A | +1 | A |
| 02 | B | +2 | B |
| 03 | C | +3 | C |
| 04 | D | $+4$ | D |
| 05 | E | +5 | E |
| 06 | F | +6 | F |
| 07 | G | +7 | G |
| 10 | H | +8 | H |
| 11 | I | $+9$ | I |
| 12 | J | -1 | J |
| 13 | K | -2 | K |
| 14 | L | -3 | L |
| 15 | M | -4 | M |
| 16 | N | -5 | N |
| 17 | 0 | -6 | 0 |
| 20 | P | -7 | P |
| 21 | Q | -8 | Q |
| 22 | R | -9 | R |
| 23 | S | 02 | S |
| 24 | T | 03 | T |
| 25 | U | 04 | U |
| 26 | v | 05 | V |
| 27 | W | 06 | W |



| G-21 <br> Internal <br> Representation | G-21 Character | Punch Card Hole Pattern | Model 29 Keypunch Character |
| :---: | :---: | :---: | :---: |
| 63 | $\wedge$ | +68 | + |
| 64 | $<$ | -58 | ) |
| 65 | \$ | -38 | \$ |
| 66 | > | -68 | ; |
| 67 | ; | 48* | (3) |
| 70 | ( | 048 | \% |
| 71 | [ | 058 | - |
| 72 | ] | 068 | > |
| 73 | ) | +48 | $<$ |
| 74 | $\downarrow$ | 78 | " |
| 75 | $\uparrow$ | +28 | $\notin$ |
| 76 | : | 028 | 0-2-8 |
| 77 | ' | 58 | , |
| 160 | Tab | +-2 |  |
| 161 | Car Ret | + 3 |  |
| 166 | Bksp | -02 |  |
| 167 | Unlock | -03 |  |
| 170 | EOM | -04 |  |
|  | job card \$ | +-89 |  |
| * Model 26 keypunch character ' . |  |  |  |
| Note: The CC-1 <br> /62 may | and teletypes do used as a no-op | have the ch | $\text { acter } \neq$ |

30. LIST OF G-21 SHIFT MULTIPLIERS

| Left Shift | Number | Right Shift |
| :---: | :---: | :---: |
| 1 | 0 | 0000000001 |
| 2 | 1 | 1010000004 |
| 4 | 2 | 1010000002 |
| 10 | 3 | 1010000001 |
| 20 | 4 | 1020000004 |
| 40 | 5 | 1020000002 |
| 100 | 6 | 1020000001 |
| 200 | 7 | 1030000004 |
| 400 | 8 | 1030000002 |
| 1000 | 9 | 1030000001 |
| 2000 | 10 | 1040000004 |
| 4000 | 11 | 1040000002 |
| 10000 | 12 | 1040000001 |
| 20000 | 13 | 1050000004 |
| 40000 | 14 | 1050000002 |
| 050000001 | 15 | 1050000001 |
| 050000002 | 16 | 1060000004 |
| 050000004 | 17 | 1060000002 |
| 060000001 | 18 | 1060000001 |
| 060000002 | 19 | 1070000004 |
| 060000004 | 20 | 1070000002 |
| 070000001 | 21 | 1070000001 |
| 070000002 | 22 | 1100000004 |
| 070000004 | 23 | 1100000002 |
| 100000001 | 24 | 1100000001 |
| 100000002 | 25 | 1110000004 |
| 100000004 | 26 | 1110000002 |
| 110000001 | 27 | 1110000001 |
| 110000002 | 28 | 1120000004 |
| 110000004 | 29 | 1120000002 |
| 120000001 | 30 | 1120000001 |
| 120000002 | 31 | 1130000004 |

31. OCTAL-DECTMAL CONVERSION TABLES

| Decimal | Octal | Octal | Decimal |
| :---: | :---: | :---: | :---: |
| 10 | 12 | 10 | 8 |
| 20 | 24 | 20 | 16 |
| 30 | 36 | 30 | 24 |
| 40 | 50 | 40 | 32 |
| 50 | 62 | 50 | 40 |
| 60 | 74 | 60 | 48 |
| 70 | 106 | 70 | 56 |
| 80 | 120 |  |  |
| 90 | 132 | 100 | 64 |
|  |  | 200 | 128 |
| 100 | 144 | 300 | 192 |
| 200 | 310 | 400 | 256 |
| 300 | 454 | 500 | 320 |
| 400 | 620 | 600 | 384 |
| 500 | 764 | 700 | 448 |
| 600 | 1130 |  |  |
| 700 | 1274 | 1000 | 512 |
| 800 | 1440 | 2000 | 1024 |
| 900 | 1604 | 3000 | 1536 |
|  |  | 4000 | 2048 |
| 1000 | 1750 | 5000 | 2560 |
| 2000 | 3720 | 6000 | 3072 |
| 3000 | 5670 | 7000 | 3. 584 |
| 4000 | 7640 |  |  |
| 5000 | 11610 | 10000 | 4096 |
| 6000 | 13560 | 20000 | 8192 |
| 7000 | 15530 | 30000 | 12288 |
| 8000 | 17500 | 40000 | 16384 |
| 9000 | 21450 | 50000 | 20480 |
|  |  | 60000 | 24576 |
| 10000 | 23420 | 70000 | 28672 |
| 20000 | 47040 |  |  |
| 30000 | 72460 | 100000 | 32768 |


|  | Sudo | Section | Sudo | Section | Sudo | Section |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ADC | 11 | LDR | 26 | SET | 19 |
| - | ALF | 13 | LEN | 9 | SIZ | 27 |
|  | BNC | 21 | LFN | 16 | SSC | 17 |
| - | BRA | 17 | LIN | 7 | SXX | 14 |
|  | BRD | 17 | LIS | 7 | TBT | 20 |
|  | BRV | 17 | LWD | 11 | TB2 | 20 |
|  | BYP | 21 | MAC | 17 | TB3 | 20 |
|  | CHK | 9 | MAD | 17 | TC8 | 26 |
|  | CKS | 18 | MON | 25 | TD8 | 26 |
|  | CLW | 11 | MTT | 8 | TIM | 7 |
|  | COA | 14 | NAM | 13 | TLC | 26 |
|  | COM | 7 | NON | 15 | TOF | 7 |
|  | CON | 15 | OCT | 7 | TOP | 7 |
|  | CPY | 27 | OPA | 25 | TYP | 25 |
| $\bigcirc$ | CRD | 25 | OPM | 7 | VAR | 17 |
|  | CSR | 18 | OPT | 27 | WRD | 11 |
|  | CSS | 21 | OUI | 15 | ZEC | 18 |
|  | DBG | 18 | OUT | 8 | 2RO | 27 |
|  | DEC | 7 | PAG | 7 | 64K | 27 |
|  | DEF | 9 | PBC | 22 | *** | 10 |
|  | DMP | 7 | PFC | 25 |  |  |
|  | Ent | 10 | PFN | 16 |  |  |
|  | ERA | 26 | PIE | 18 |  |  |
|  | ERO | 26 | POP | 17 |  |  |
|  | ERR | 18 | PRT | 9 |  |  |
|  | EXR | 26 | PSH | 17 |  |  |
|  | FIN | 17 | PUL | 9 |  |  |
| * | FLG | 18 | PVE | 7 |  |  |
|  | FPC | 12 | RBC | 22 |  |  |
|  | FPL | 12 | RD8 | 26 |  |  |
|  | HPC | 12 | REF | 1.5 |  |  |
| $\sim$ | HPL | 12 | REL | 9 |  |  |
|  | ITR | 19 | RET | 8 |  |  |
|  | LBL | 9 | RXA | 14 |  |  |
|  | LC8 | 26 | SCP | 10 |  |  |

33. LIST OF PREDEFINED LABELS
|0 to | 100 Monitor references, except:
| 36 Base address of MTHAT symbol table
Subroutine entry point to MTHAT
Base address of a table of left shift multipliers, from $\leftrightarrow 5$ to $\leftrightarrow 31$, inclusive

Base address of a table of right shift multipliers, from $\rightarrow 0$ to $\rightarrow 31$, inclusive Base address of a table of single bits, from $\$ 0$ to $\$ 31$, inclusive

Base address of a table of flag bits, from F0 to F3, inclusive Base address of the alphanumeric representations of all the identifiers used by MTHAT, stored one character per word in the same order as the MTHAT identifier table

Size of table 14
Base address of a table of G-21 instruction memonics, the 3 characters of each memonic stored right-justified in the word

Size of table '6
Base address of a table of G-21 opcodes and standard modes, appearing in the same order as table '6

Base address of a table of MTHAT sudo memonics, the 3 characters of each memonic stored right-justified in the word

Size of table '9
Base address of a table of G-21 register and line command mnemonics, stored right-justified in the word

| $\sim$ | '12 | Size of table '11 |
| :---: | :---: | :---: |
|  | 113 | Base address of a table of register numbers and line |
|  |  | commands, appearing in the same order as table '11 |
| - | 114 | Sudo trap transfer location |
| * | 115 | Base address of MTHAT card image, stored four characters |
|  |  | per word into 21 words |
|  | '16 | Base address of MTHAT |
|  | ${ }^{17}$ | Subroutine: Convert (ACC) to label for symbolic dis- |
|  |  | assembly |
| $\sim$ | '18 | Subroutine: Write a logical file table entry |
|  | 19 | Subroutine: Read a logical file table entry |
|  | '20 | First location after the end of storage used by the MTHAT |
|  |  | run-time subroutines and tables |
|  | '21 | Switch: Upper core request |
|  | ${ }^{\prime 2}$ | Subroutine: Write a disc or tape file |
|  | '23 | Subroutine: Read a disc or tape file |
|  | '24 | Subroutine: Test if (ACC) is within user memory |


[^0]:    * For example: FLPL [1] , FORMAC [2], ALPAK [3], the earlier version of FORMULA ALGOL [4], and AMBIT [5].

[^1]:    The row-binary cards that were punched by PBC should follow immediately after the RBC card, with no blank cards intervening. Two blank cards should be placed after the row-binary deck before the remaining MTHAT cards.

